

Cathedrals as Solar Observatories

The Role of the Church in Restraining and Advancing the Science of Astronomy

Dr. Dan Fleisch

Professor Emeritus of Physics

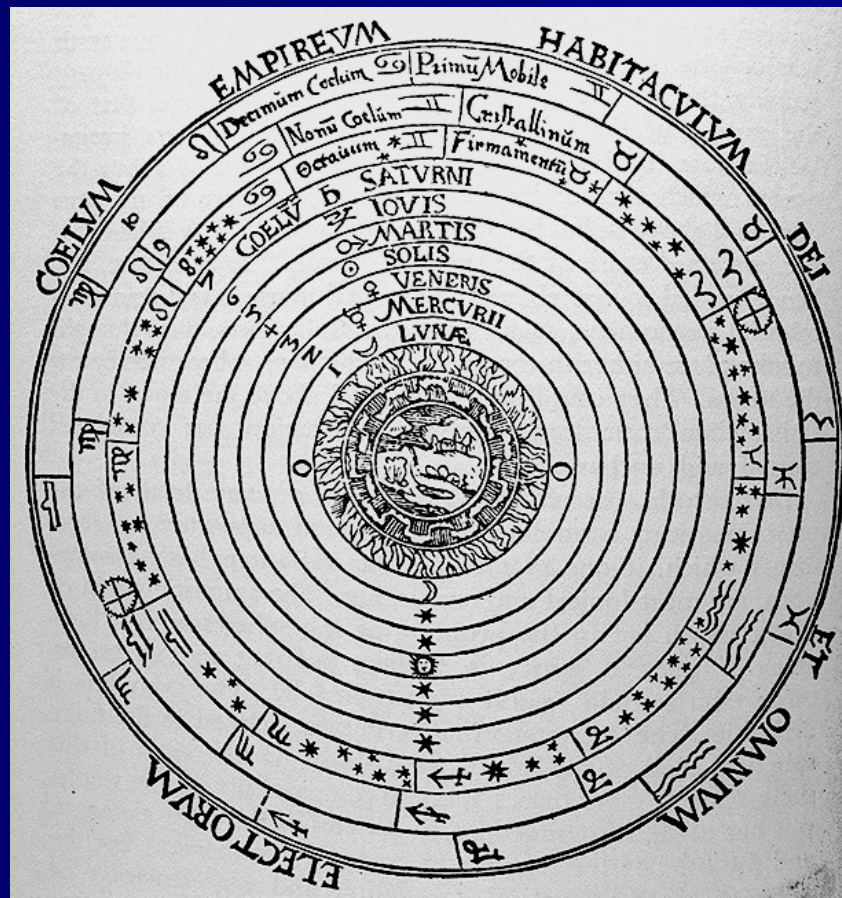
Wittenberg University

Grand Canyon Astronomer in Residence 2022 & 2023

March 31st, 2024

The Universe of the ancients

Geocentric Model



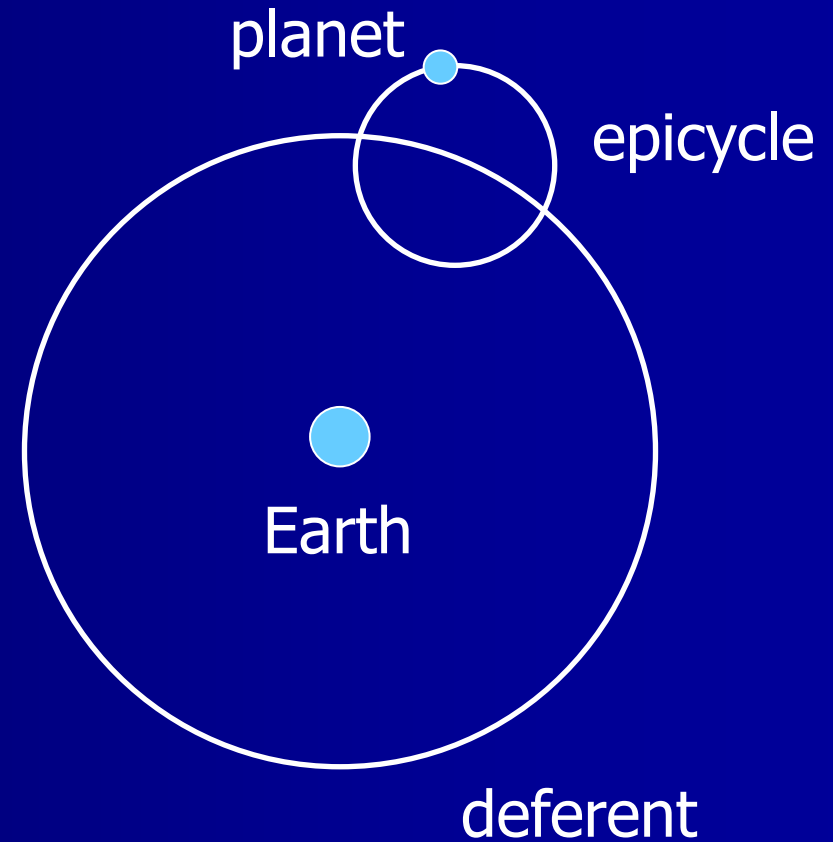
The problem of retrograde motion



http://www.star.ucl.ac.uk/~apod/apod/image/0604/Mars2005_6_tezel_c51.jpg

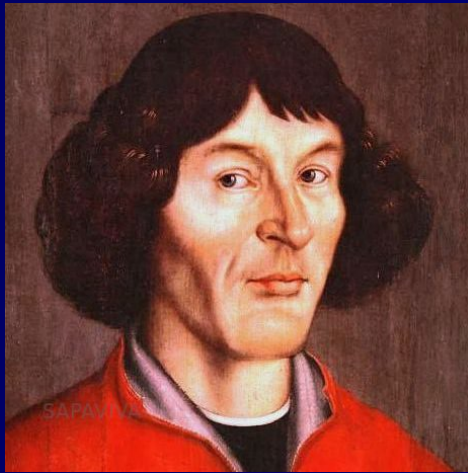
Ptolemy's solution

Claudius Ptolemaeus
c. 90 – c. 168 AD

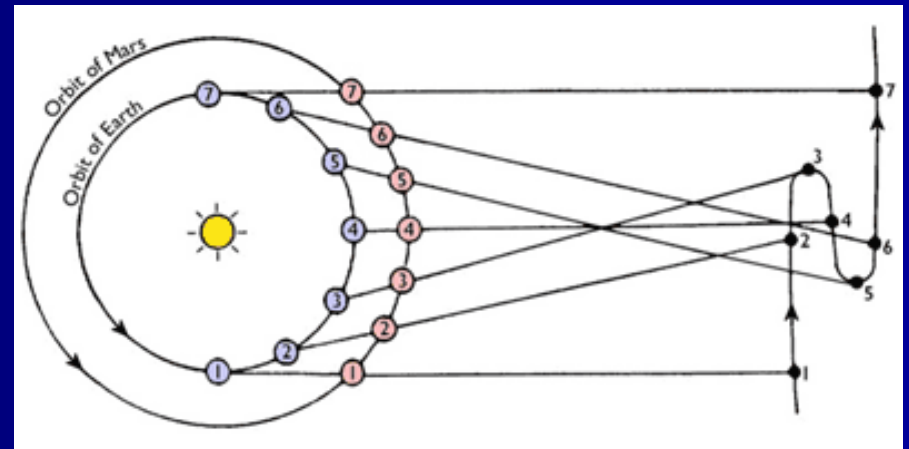


1500 Years Later: Copernicus' Solution

Nicolaus Copernicus
1473 - 1543 AD



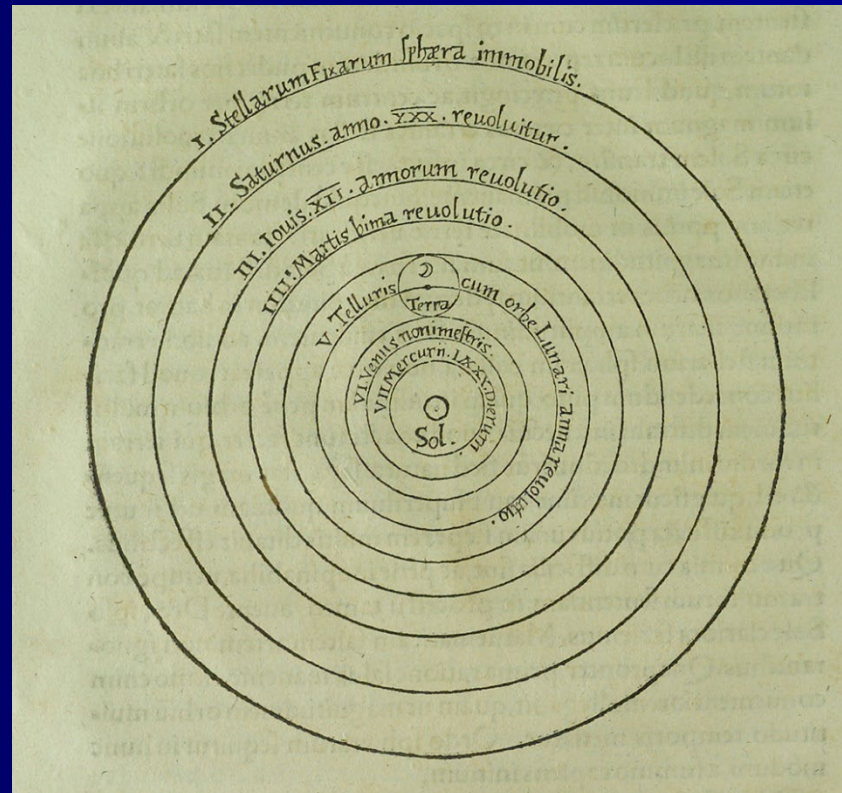
<https://www.sapaviva.com/wp-content/uploads/2017/06/23S.-Nicolaus-Copernicus-1473-1543-463x463.jpg>



<https://demos.smu.ca/images/stories/Pics/retrograde/retrograde.gif>

The Universe of Copernicus

Heliocentric Model



https://maa.org/sites/default/files/images/upload_library/46/Swetz_2012_Math_Treasures/Lehigh_University/Lehigh_Copernicus/Lehigh_4_065_left.jpg

Why the big change?

The traditional explanation:

- Increasing errors in predicted positions
- Increasing complexity of Ptolemaic model
- Wonderful simplicity of Copernican model
- Improved accuracy of Copernican model

Just four problems

- No increasing errors in Ptolemy
- No increasing complexity in Ptolemy
- Copernican model not so simple
- Copernican model not so accurate

Ptolemy: A closer look

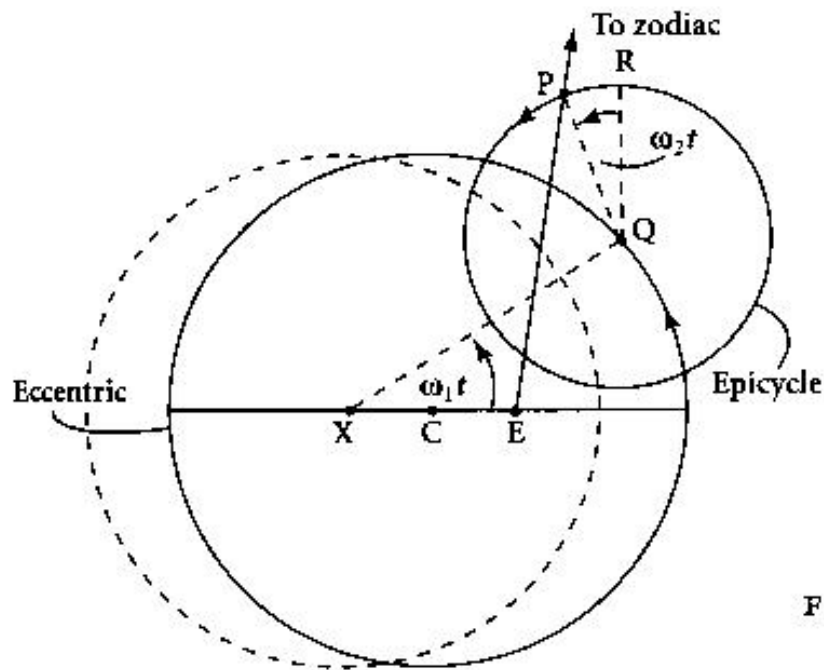
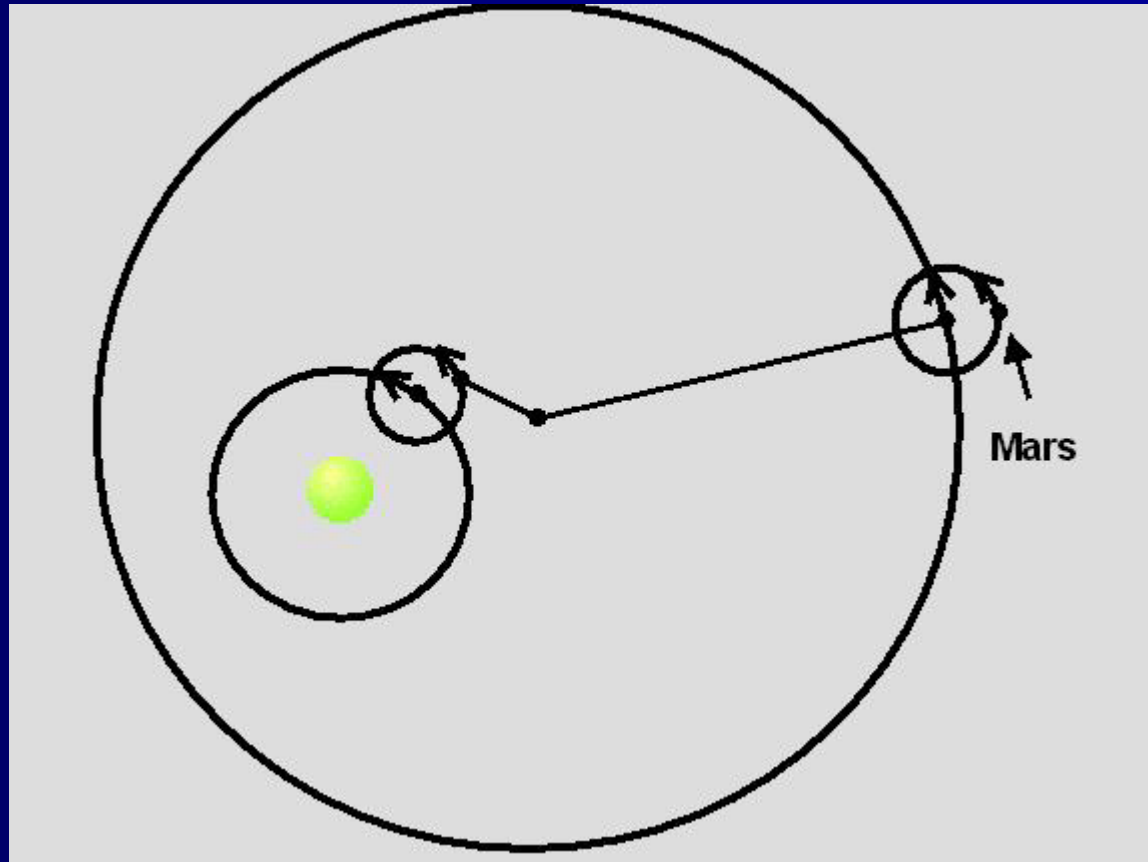


FIG. 3.15. Ptolemaic device of eccentric and epicycle.

Copernicus: A closer look



No simple explanation

The actual causes of the shift from geocentric to heliocentric are far more subtle.

To understand those causes, it's necessary to know their context.

Context: The Renaissance

Middle Ages

500 to 1400 AD

Modern Era

1700 AD –
Present Day

Renaissance

1400 – 1700 AD

“Renaissance” translates as “Rebirth”

Europe during the Renaissance

Exploration

Columbus

Vasco da Gama

Magellan

Reformation

Luther

Knox

Art and Science

da Vinci

Michelangelo

Copernicus

Kepler

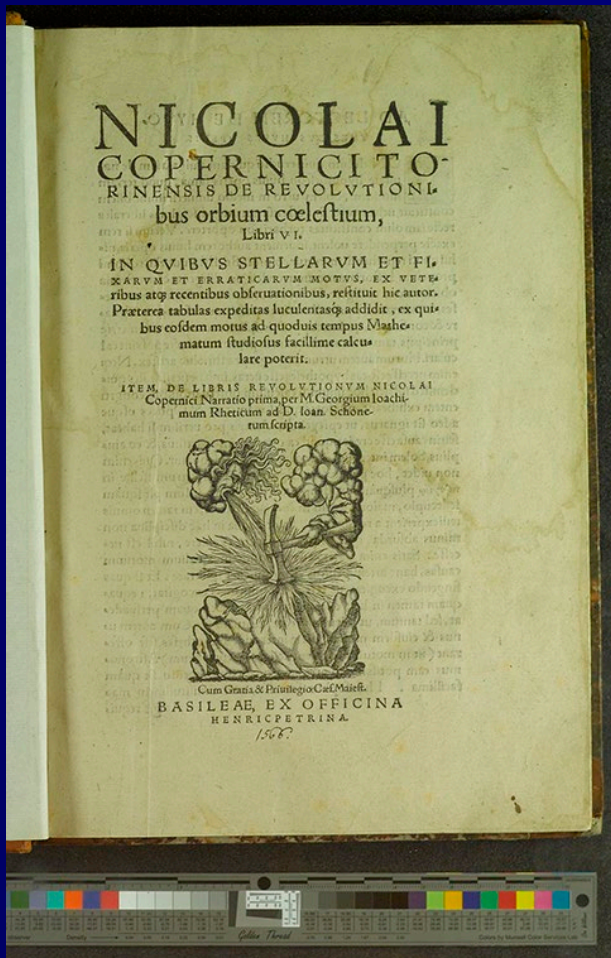
Galileo

Inquisition

Spanish

Roman

De Revolutionibus



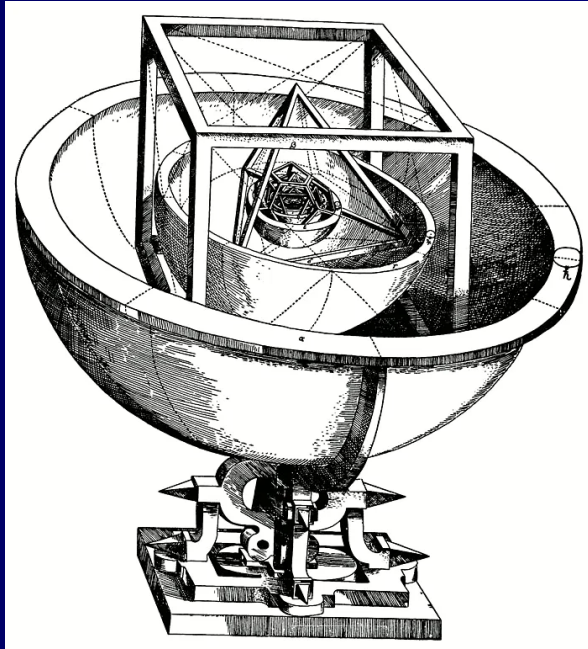
Copernicus' primary motivation:

He felt Ptolemy's equant was an inelegant solution.

And Copernicus had the expertise and free time to seek an alternative.

https://maa.org/sites/default/files/images/upload_library/46/Swetz_2012_Math_Treasures/Lehigh_University/Lehigh_Copernicus/Lehigh_4_064.jpg

Kepler partially agrees



Wait – Who's Kepler?

<https://www.worldhistory.org/img/r/p/1500x1500/17841.png.webp?v=1710877626>

November 11, 1572



A "new star" appears
in the constellation Cassiopeia

In Denmark, alchemist Tycho Brahe
takes note

Hmmm.

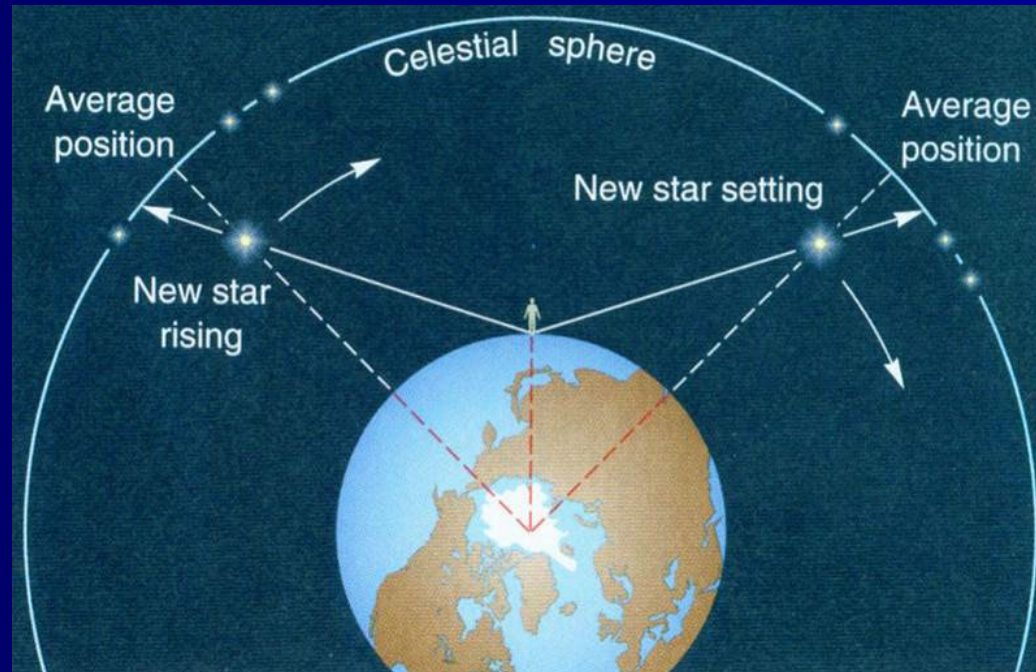


Fleisch

<http://galileo.rice.edu/images/people/brahe.gif>

What Bugged Tycho

The "new star" didn't show any PARALLAX as it moved across the sky!



And only very distant objects don't show parallax.

Trouble for Aristotle

According to Aristotle:

- the celestial sphere is perfect
- nothing ever changes on the sphere
- objects "below the Moon" can change

But Tycho knew:

- the heavens DID change when the new star appeared
- the new star MUST be very far away



Right Guy, Right Place, Right Time

Columbus

Copernicus

Luther

By 1578, Tycho had become the most famous astronomer in the world



Tycho Brahe

Tycho was the first "modern" observational astronomer – he loved taking data

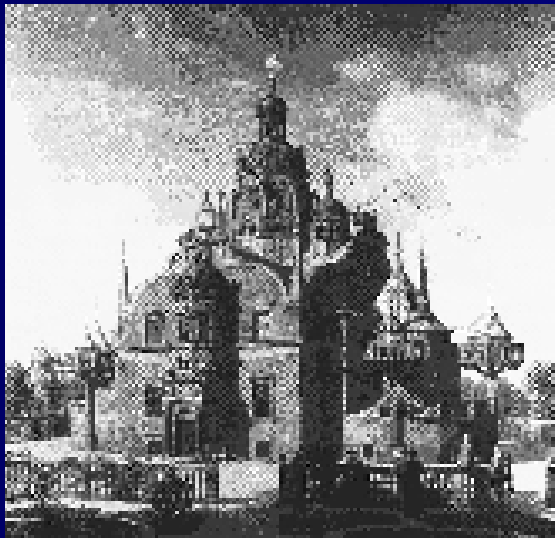
Kepler

Galileo

Newton

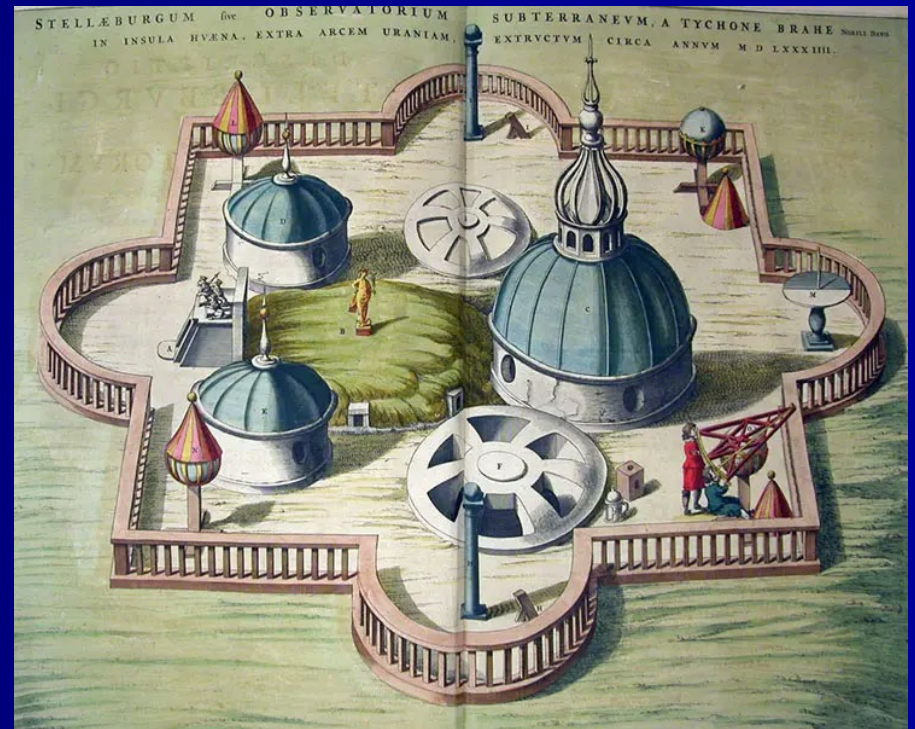
Tycho Brahe at Hven

King of Denmark: "How about a castle?"



<https://faculty.wcas.northwestern.edu/inform/ocom/Ideas/graphics/uraniborg1.jpg>

Brahe: "What the hell, I'll take the whole island."



<https://assets-us-01.kc-usercontent.com/9dd25524-761a-000d-d79f-86a5086d4774/742ebf9a-203d-4d67-851c-8d451a415a90/brahe2.jpg?w=741&h=600&auto=format&q=75&fit=crop>

Uraniborg – "Celestial Castle"

Tycho Brahe outfitted Uraniborg with everything any astronomer would want:

1. Cylindrical observation towers with removable roofs
2. 38-ft brass and oak quadrant for measuring angles
3. 5-ft brass sphere on which star positions could be engraved
4. Scientific library
5. Multiple galleries and workshops
6. Portrait gallery showing eight greatest astronomers (including Tycho himself and his unborn descendant)
7. Jepp the dwarf

Brahe's "Data Product"

Without benefit of a telescope, Brahe consistently measured star and planet positions to within 1 arc minute ($1/60^\circ$).

Over 20 years, Brahe catalogued the positions of over 770 stars and all five known planets.



Enter Kepler



- German mathematician
- Born 1571, died 1630
- Dysfunctional family life
- Great supporter of Copernicus
- Became Brahe's assistant one year before Brahe's death

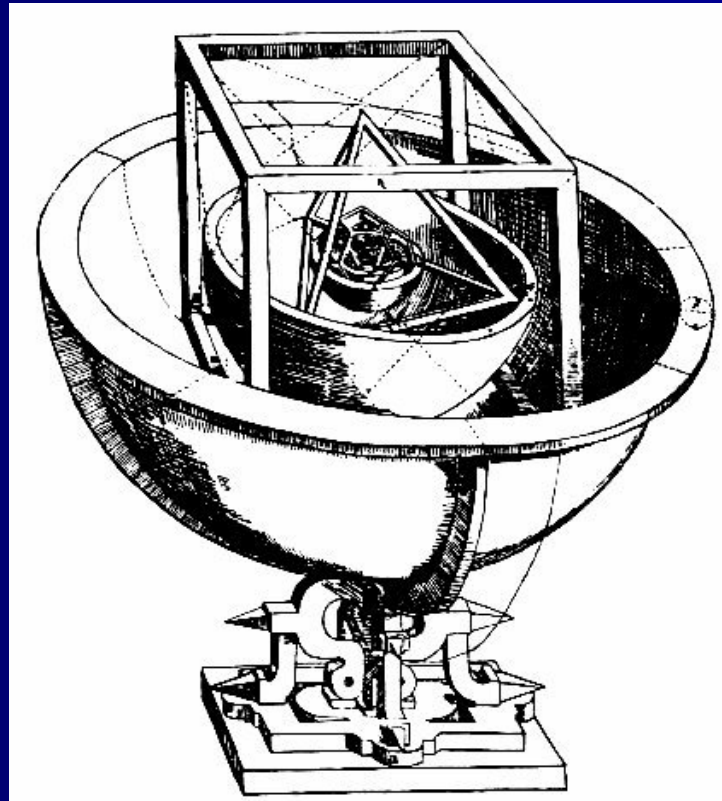
https://www.esa.int/var/esa/storage/images/esa_multimedia/images/2000/10/johannes_kepler_1571-1630/9233019-6-eng-GB/Johannes_Kepler_1571-1630_pillars.gif

Whacky Ideas, Great Ideas

Wacky

5 planets,
5 "perfect" shapes

SHAPES DEFINE
ORBITS!



Great

Observations
of planet's
positions can
help us
understand
the nature
of their orbits

Kepler NEEDED
all of Tycho's
data

Kepler Gets Brahe's Data



<https://i.ebayimg.com/images/g/9q0AAOSwDSJb8fiU/s-l1600.jpg>

Brahe Brood

Kepler Clan

And the winner is ... Johannes Kepler!

Kepler Prevails

Using Tycho Brahe's data, Kepler derived the "Laws of Planetary Orbits" that changed forever the way astronomers look at the heavens.

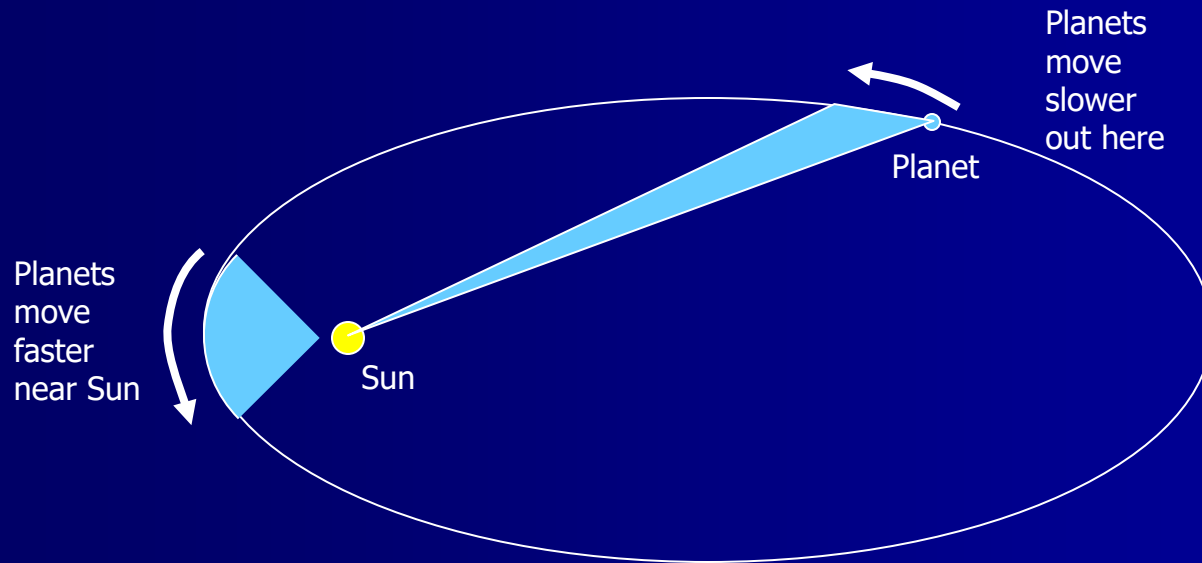
Gone were the unchanging "Celestial Sphere" and perfect circles of Aristotle.

Now we have the true figure of an orbit:

The ELLIPSE!

Kepler's 1st and 2nd Laws

1st Law: Planetary orbits are ellipses



2nd Law: Equal areas covered in equal times

Kepler's Third Law

$$P^2 = a^3$$

Period of Revolution
(in years)



Distance from Sun
(in Astronomical
Units)



Technology Rears Its Head

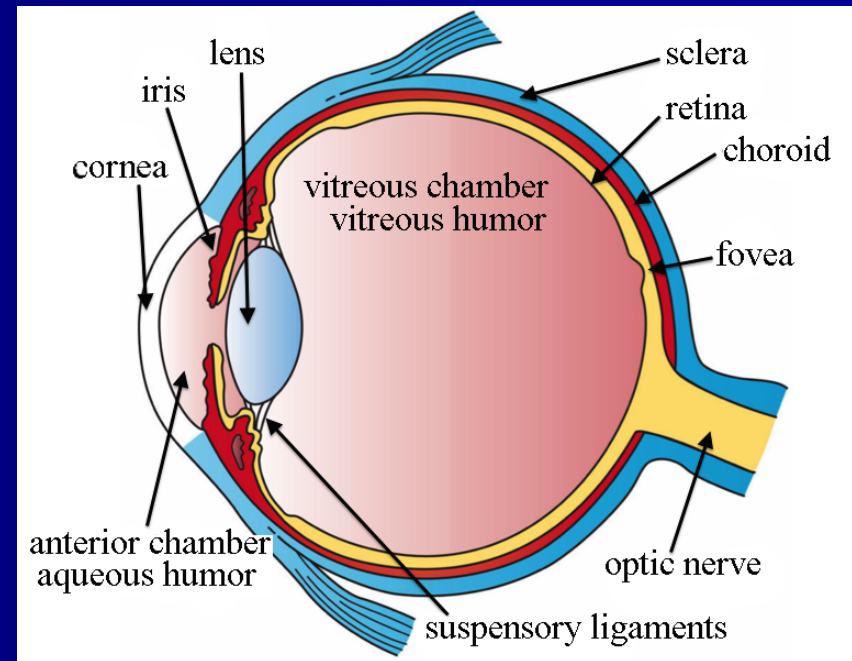


https://catalogue.museogalileo.it/images/cat/oggetti_944/0554_3253_0429-018_944.jpg

Why This Technology Matters

Three ways in which Nature can hide from our sight:

- Tiny angular size
- Extreme faintness
- Wavelength beyond our detection range



<https://harvardeye.com/wp-content/uploads/2018/08/Diagram-of-the-Eye.png>

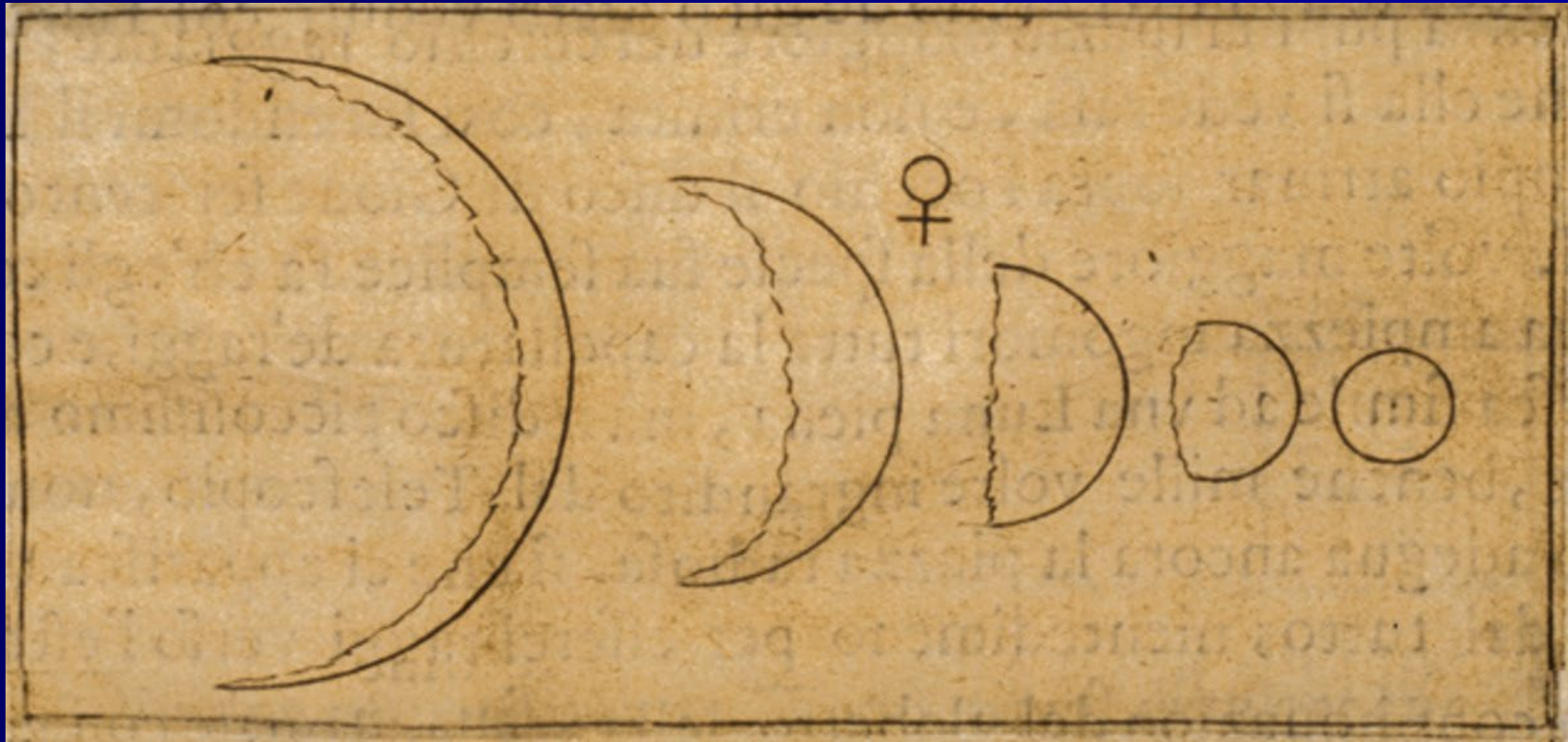
Galileo Looks Up in 1609



Oh,
the things
you'll see

https://3.bp.blogspot.com/-yuda7JPsdE/W4B5XQFWqDI/AAAAAAAAAKbU/QGc0YjYFc-YfH1BVP_2hA0P2FgmFRcoKwCLcBGAs/s1600/Bertini_fresco_of_Galileo_Galilei_and_Doge_of_Venice.jpg

Venus Has Phases



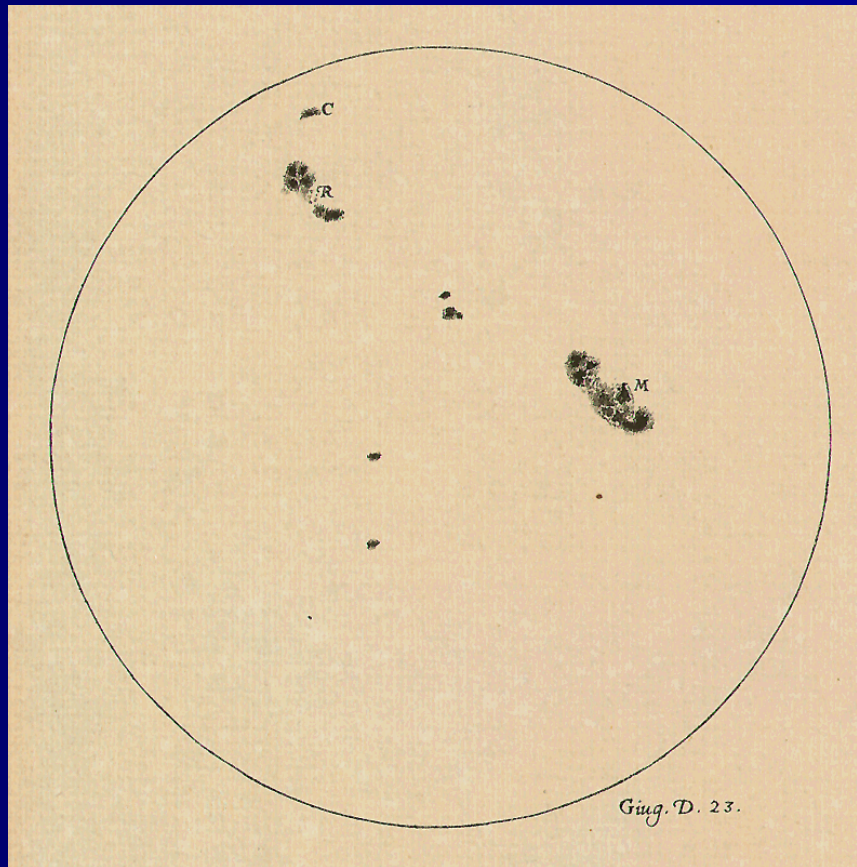
https://images.saymedia-content.com/.image/t_share/MTc1Nzg1MTc0NDUyMjE2ODg3/galileo-galilei-discovers-the-moons-of-jupiter-and-the-phase-of-venus.jpg

The Moon Has Craters



http://galileo.rice.edu/images/things/g_sidnun_moon-t.gif

The Sun Has Spots



Jupiter Has Moons

OBSERVAT. SIDERAE

berit: Iuppiter à sequenti occidua min. 5. hęc verò à reliqua occidentaliori min. 3. erant omnes claf-

Ori. * ○ * * Occ.

dem proximè magnitudinis, fatis conspicuę, & in eadem recta linea exquisitè secundum Zodiaci ductum.

Die decimsseptima H. 1. duę aderant Stellę, orientalis vnā à Ioue distans min. 3. occidentalis altera distans

Ori. * ○ * Occ.

min. 10. hęc erat aliquanto minor orientali. Sed hora 6. orientalis proximior erat Ioui distabat nempe mi. 6. sec. 50. occidentalis verò remotior fuit, scilicet min. 12. Fuerunt in vtraque obseruatione in eadem recta, & ambę fatis exiguę, præsertim orientalis in secunda obseruatione.

Die 18. Ho. 1. tres aderant Stellę, quarum duę occidentales, orientalis verò vnā distabat orientalis à Ioue

Ori. * ○ * * Occ.

min. 3. Occidentalis proxima m. 2. occidentalis reliquę aberat à media m. 8. Omnes fuerunt in eadem recta ad vnguem, & eiusdem ferè magnitudinis. At Hora 2. Stellę viciniores paribus à Ioue aberant intersticij: occidentalis enim aberat ipsa quoque m. 3. Sed Hora 6. quarta Stellula visa est inter orientaliorem & Iouem in tali configuratione. Orientalior distabat à sequenti m. 3. sequenti à Ioue

RECENS HABITAE. 26

Ioue m. 1. sec. 50. Iuppiter ab occidentali sequenti m. 3.

Ori. * * ○ * * Occ.

hęc verò ab occidentaliori m. 7. erāt ferè æquales, orientalis tantum Ioui proxima reliquis erat paulo minor, erantque in eadem recta Eclipticę parallela.

Die 19. Ho. 6. m. 40. Stellę duę solimmodo occiditę à Ioue conspicuę fuerunt fatis magnę, & in eadem re-

Ori. ○ * * Occ.

cta cum Ioue ad vnguem, ac secundum Eclipticę ductū dispositę. Propinquior à Ioue distabat m. 7. hęc verò ab occidentaliori m. 6.

Die 20. Nubilosus fuit cœlum.

Die 21. Ho. 1. m. 30. Stellę tres fatis exiguę cernebantur in hac constitutione. Orientalis aberat à Ioue

Ori. * ○ * * Occ.

m. 2. Iuppiter ab occidentali sequente m. 3. hęc verò ab occidentaliori m. 7. erant ad vnguem in eadem recta Eclipticę parallela.

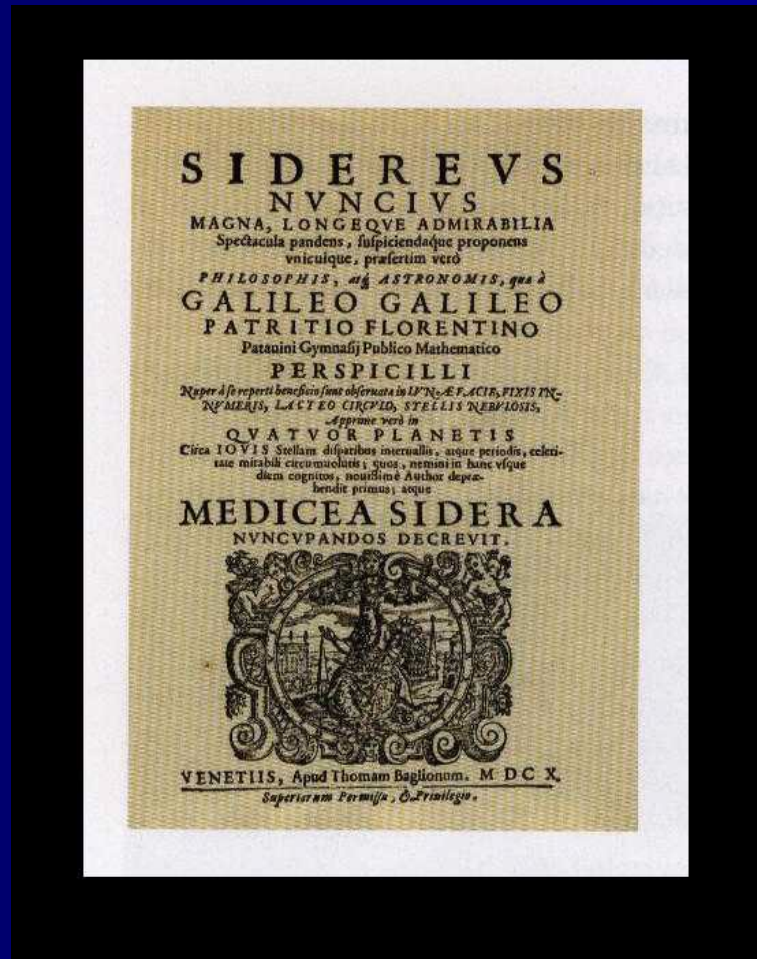
Die 25. Ho. 1. m. 30. 4. n. m. superioribus tribus noctibus cœli fuit nubibus obductum) tres apparuerūt Sed

Ori. * * ○ * Occ.

lx. Orientales duę, quarum distantia inter se, & à Ioue

G 2 æquales

The Word Is Out



SIDEREVS
NUNCIVS

Adan 5. 61. 1

MAGNA, LONGEQVE ADMIRABILIA
*Spectacula pandens, suscipiendaque proponens
unicuique, praesertim vetò*

PHILOSOPHIS, atq; ASTRONOMIS, qua à
GALILEO GALILEO
PATRITIO FLORENTINO

Pazzani Gymnasij Publico Mathematico

PERSPICILLI

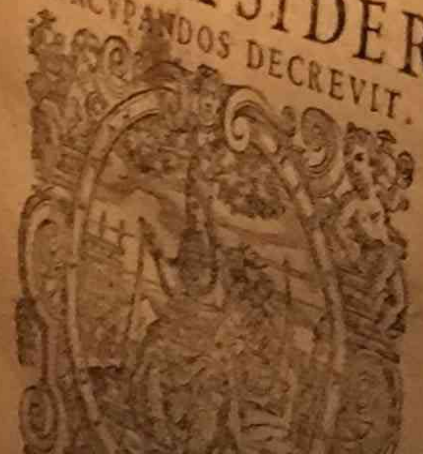
*Per quos à se reperti haec sunt obiecta in U^No, & FACIE, FIXIS IN
SYMERIS, LACTEO CIRCVLO, STELLIS NEBVLOSIS,*

Appareat vetò in

QVATVOR PLANETIS

*Com IOVIS sedem dispersos intervalla, atque periodis, celeri-
ter variabilis circumstantibus, quos, nemini in hanc usque
hanc usque, nullius in Verba depre-
hendit primari; atque*

MEDICEA SIDERA
NUNCUPANDOS DECREVIT.



Did We Hear Something About the Heavens?



A Warning Seems Warranted



The Holy Office of the Inquisition

Rough Road for Heliocentrism

Heliocentrism declared to be heretical in 1616.

Copernicus' book added to Index Librorum Prohibitorum

Galileo told to abstain from teaching or discussing his theories surrounding heliocentrism as fact.

The Teeth in the Warning: Memory of Giordano Bruno

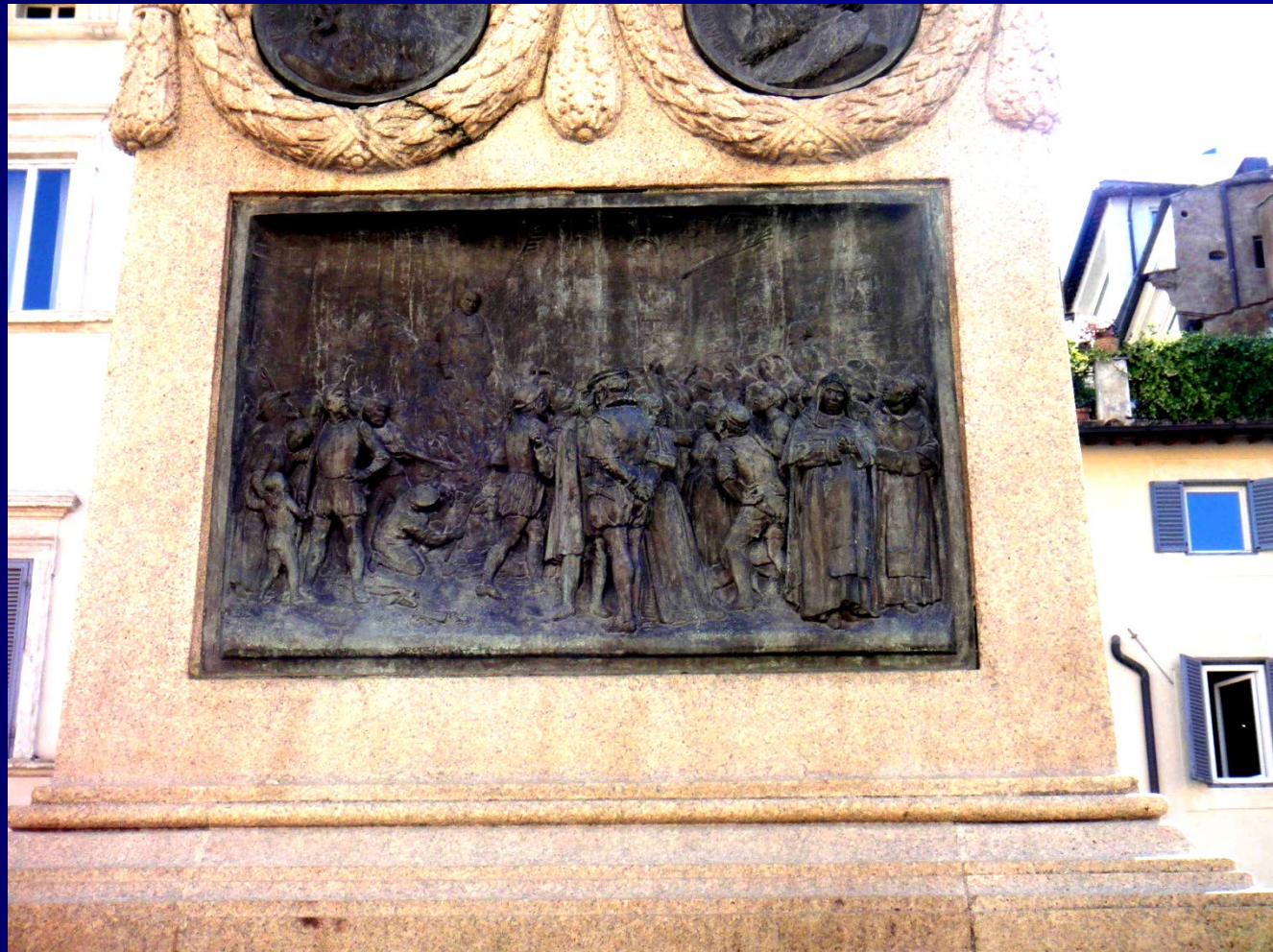
Giordano Bruno
(1548 – 1600)



Campo
dei Fiori

Fleisch

Bruno's Fate



The Warning Wears Off



DIALOGO
D I
GALILEO GALILEI LINCEO
MATEMATICO SOPRAORDINARIO
DELLO STUDIO DI PISA.
E Filosofo, e Matematico primario del
SERENISSIMO
GR. DVCA DI TOSCANA.

Doce ne i congressi di quattro giornate si discorre
sopra i due

MASSIMI SISTEMI DEL MONDO
TOLEMAICO, E COPERNICANO;

*Proponendo indeterminatamente le ragioni Filosofiche, e Naturali:
tanto per l'una, quanto per l'altra parte.*

CON PRI



VILEGI.

IN FIRENZA, Per Gio:Batista Landini MDCXXXII.

CON LICENZA DE' SUPERIORI.

Dialogue over the
Two Chief Systems
of the World

1632

Two Pretty Smart Guys and One Not So Much

Salviati: Supports Copernicus

Sagredo: Neutral (initially)

Simplicio: Supports Ptolemy and Aristotle

“pure mathematical hypothesis”

1633: The Church Isn't Buying It

Verdict: "Vehemently Suspect of Heresy"



Galileo Forced to Abjure

"I have been judged vehemently suspect of heresy, that is, of having held and believed that the sun in the centre of the universe and immoveable, and that the earth is not at the center of same, and that it does move. Wishing however, to remove from the minds of your Eminences and all faithful Christians this vehement suspicion reasonably conceived against me, I abjure with a sincere heart and unfeigned faith, I curse and detest the said errors and heresies, and generally all and every error, heresy, and sect contrary to the Holy Catholic Church."

Abjure: to renounce, repudiate, or retract, especially with formal solemnity; to recant.

Galileo's Fate: House Arrest For the Rest of His Life



The Oft-told Story

By placing Galileo under house arrest, the Church seriously restricted the advancement of astronomy and science in general.

And this is certainly accurate.

But, as usual...

...there's more to the story.

Right and Wrong

Ptolemy: Right about offset, wrong about epicycles

Copernicus: Right about heliocentrism, wrong about circular orbits

Kepler: Right about elliptical orbits, wrong about number of planets

Galileo: Right about Earth moving, wrong about tides

Trouble with Easter

Easter Sunday:

The first Sunday
after the first full Moon
after the vernal equinox.

So exactly which day is
the holiest day of our
liturgical calendar?



An Inconvenient Number

Time from one vernal equinox to the next
= 1 solar year

1 solar year = 365.2433 solar days

Another Inconvenient Number

Time from one new moon to the next
= 1 synodic month

1 synodic month = 29.53059 solar days

Growing Discrepancy

In 325 AD, the Council of Nicea set
1 year = 365.25 days

So every year, the time at which the Sun
reached a certain position in the sky would
shift by 11.2 minutes.

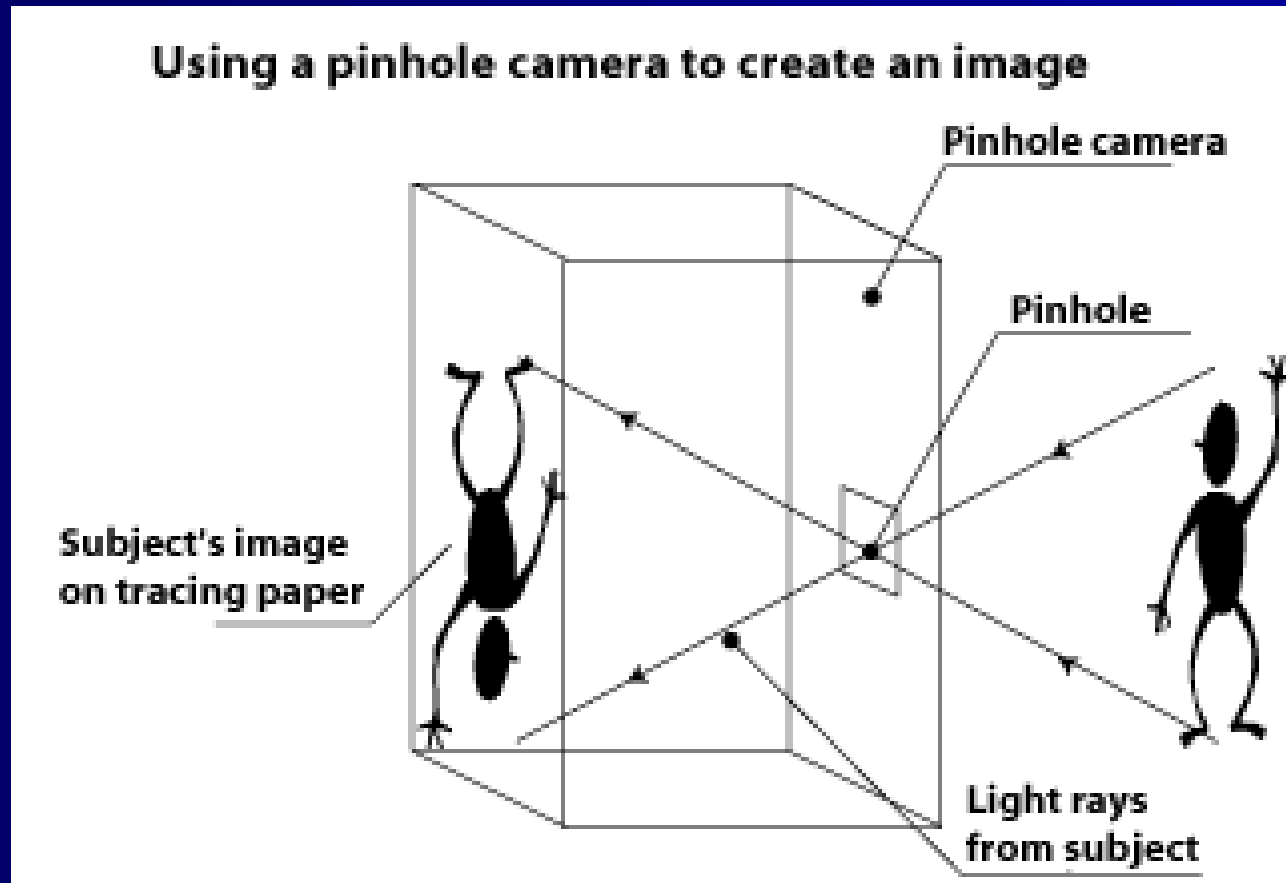
By 800 AD, the discrepancy was 3.7 days.

Vernal Equinox was falling on March 17th.

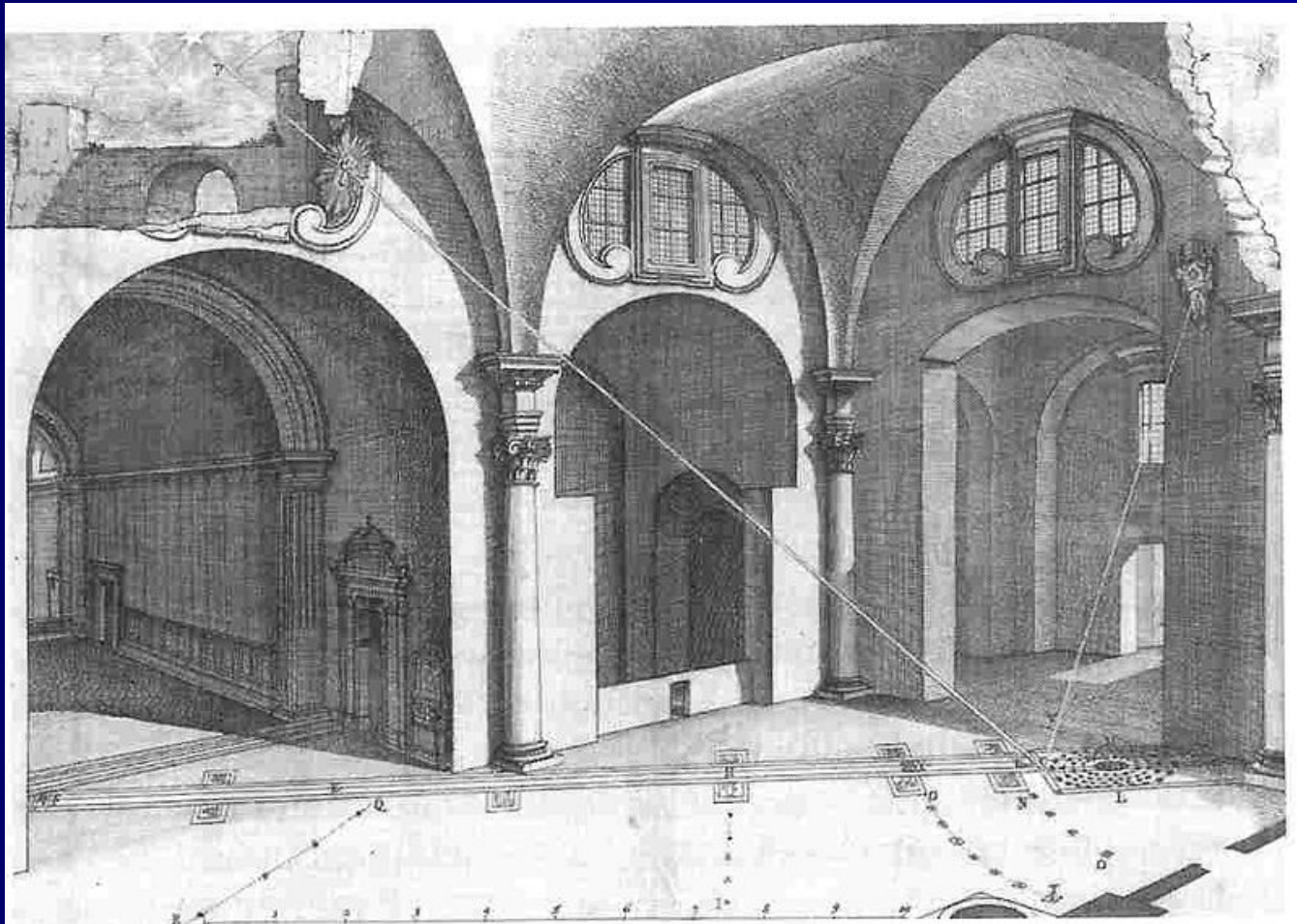
How To Settle This?



A Good Measuring Tool to Get Data on the Sun's Position



Cathedral as Observatory



The Sun in the Church, J.L. Heilbron

A Line to Track the Sun

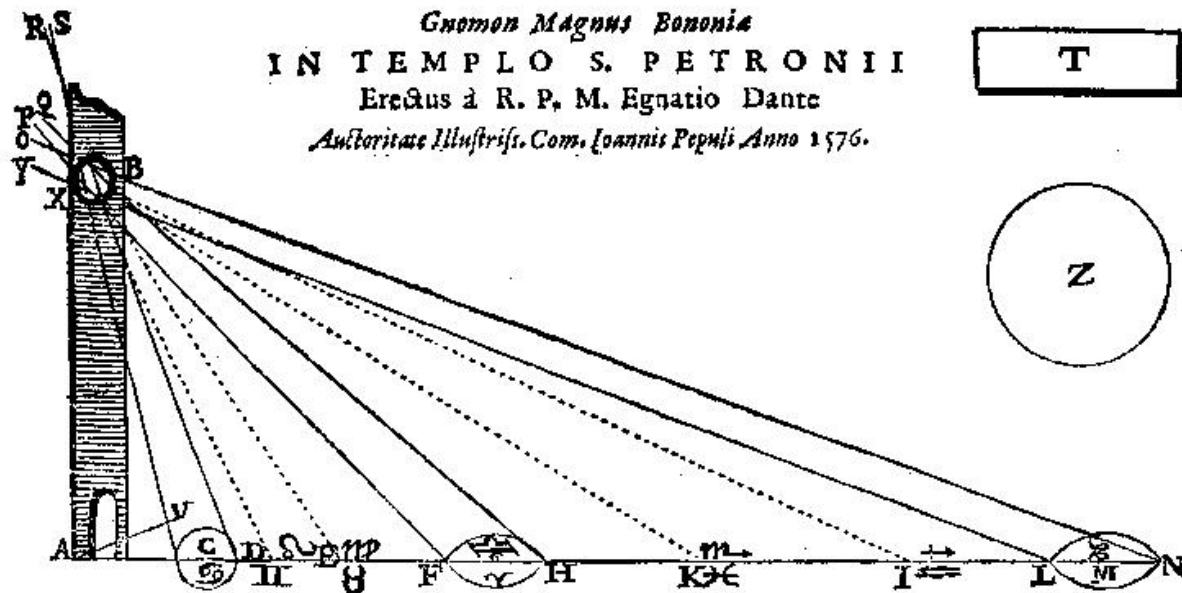


FIG. 2.31. Danti's *meridiana* in San Petronio. T is the cross-section, Z the size and shape of the hole. From Riccioli, *Almagestum novum*, 1:1 (1651), 132.

Santa Maria degli Angeli in Rome



Why this Church?

- Southern exposure

- Settled walls

- Symbolic value

Interior of Santa Maria degli Angeli

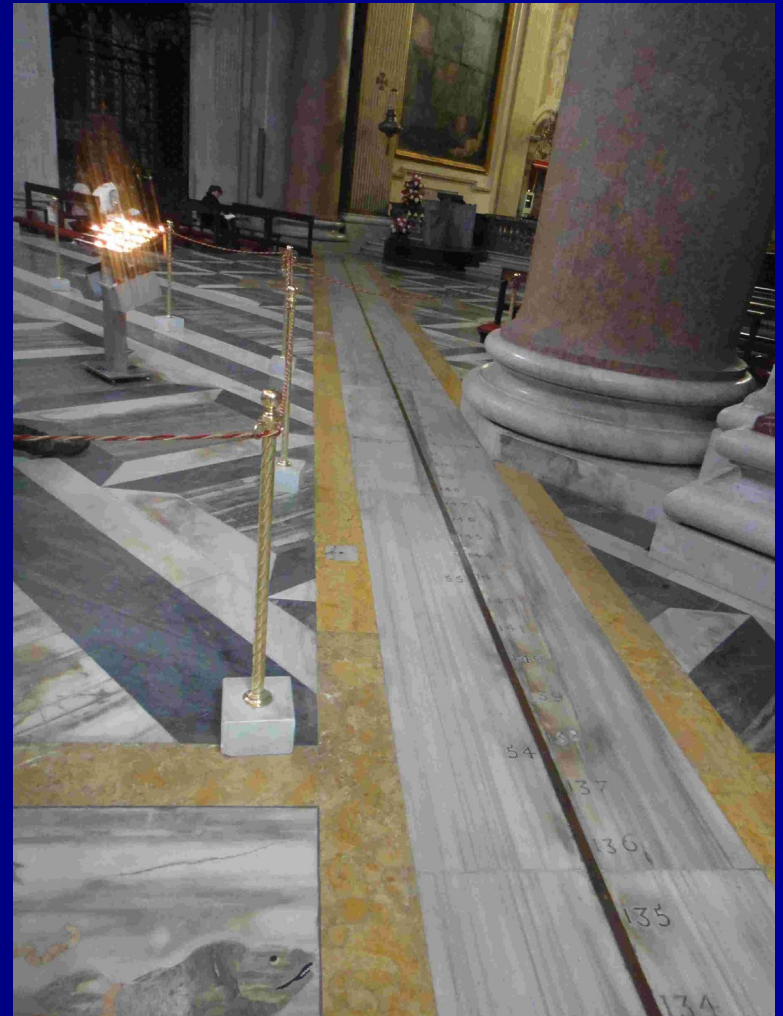


The Meridian Line

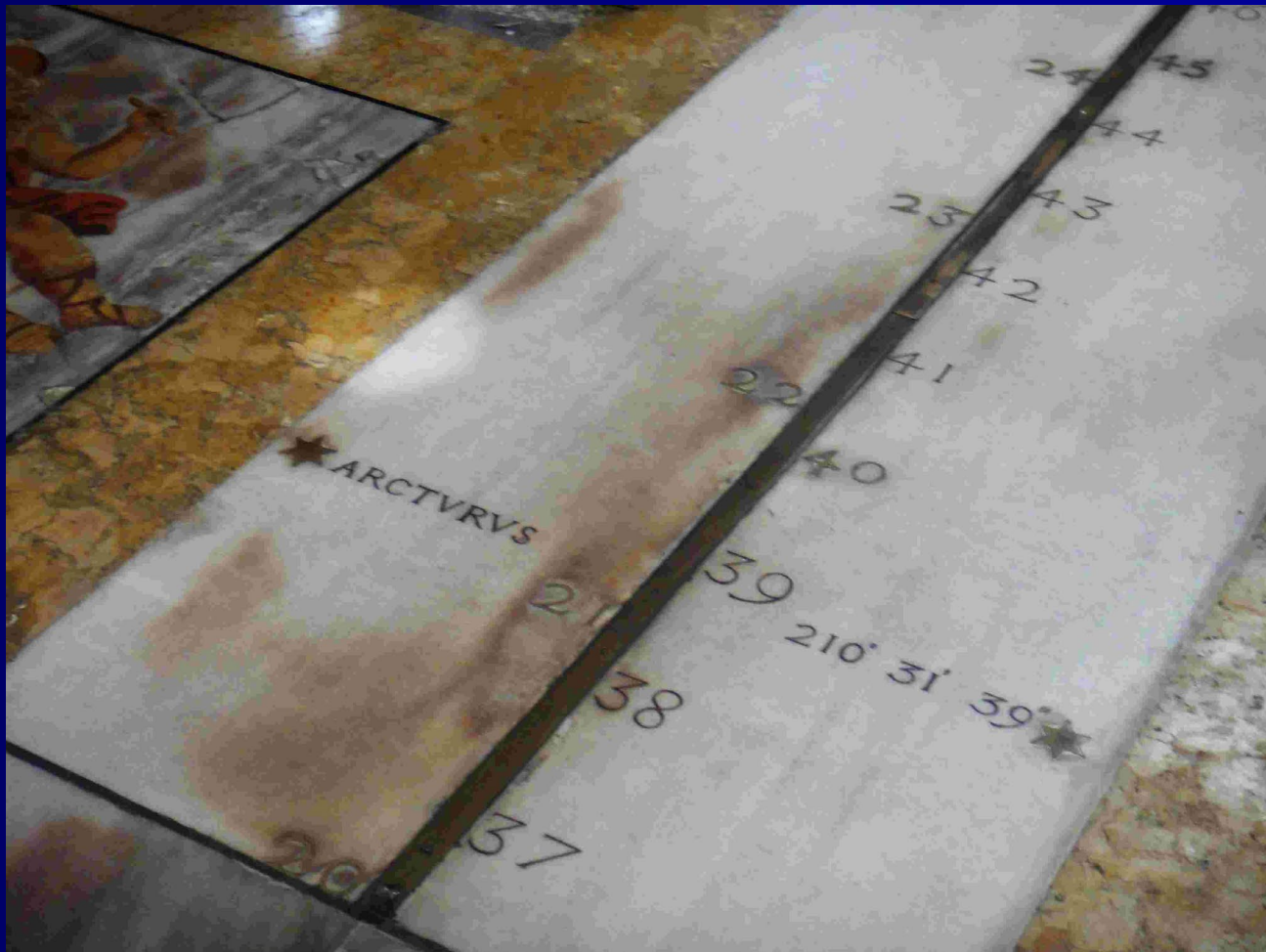


Fleisch

Completed in 1703



The Sun in the Church



Saint-Sulpice in Paris



Interior of Saint-Sulpice



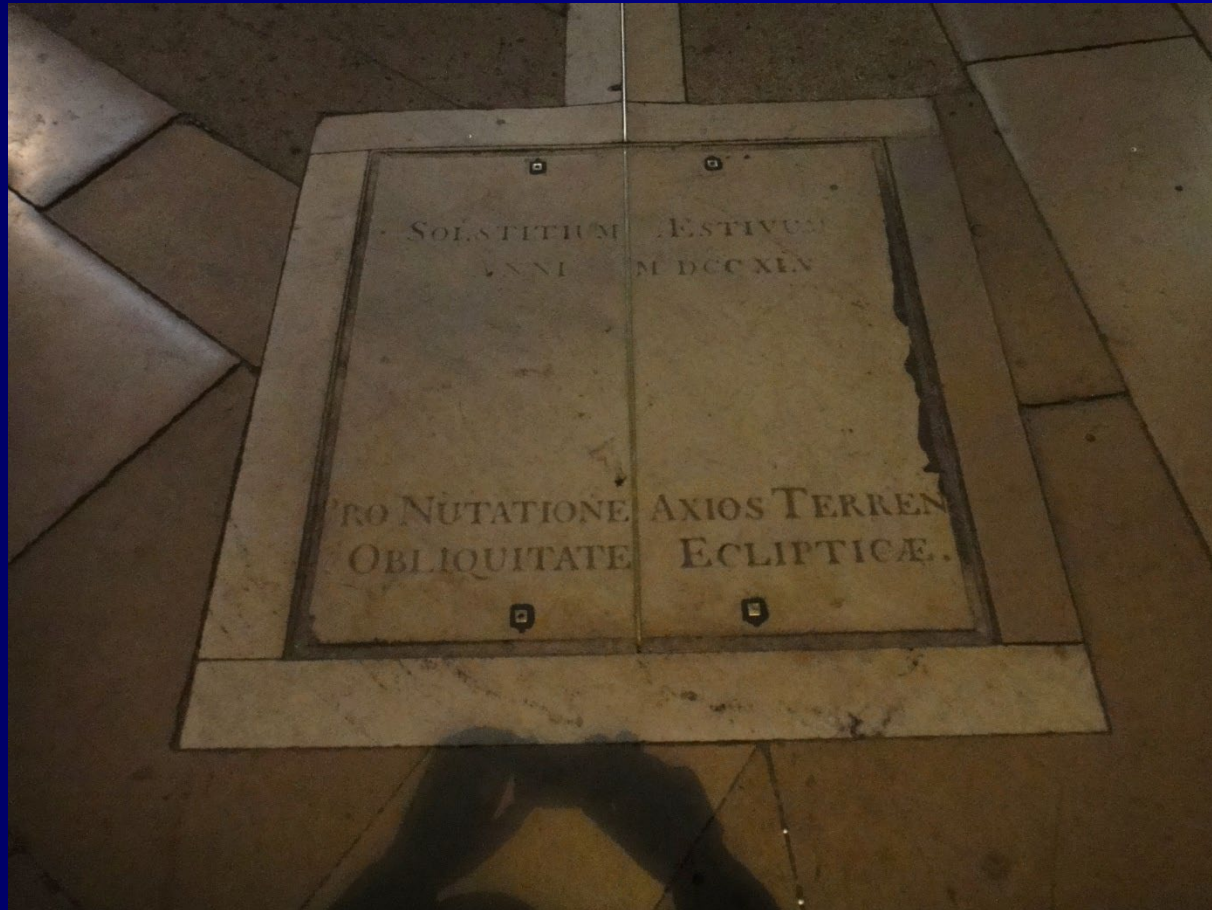
Meridian Line in Saint-Sulpice



Saint-Sulpice Pinhole



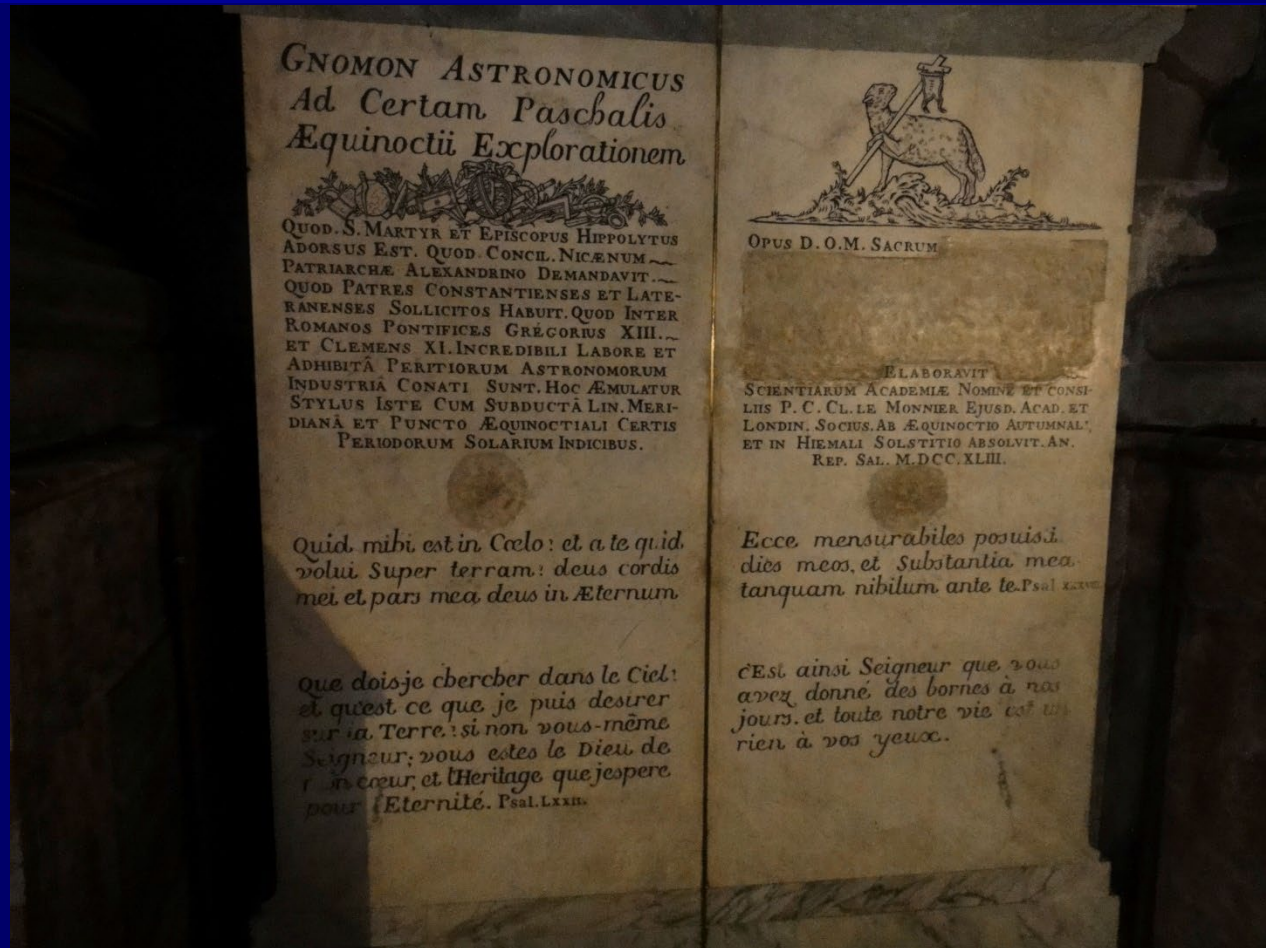
Beginning of Meridian Line



End of Meridian Line



Meridian Line Inscription



Fixing Misconceptions

NOTE

The « meridien » line materialized by a brass inlay in the pavement of this church is part of a scientific instrument built here during the 18th century. This was done in full agreement with Church authorities by the astronomers in charge of the newly-established Paris Observatory. They used it for defining various parameters of the earth's orbit. Similar arrangements have been made, for the sake of convenience, in other large churches like the Bologna cathedral where Pope Gregory XIII had preparatory studies made for the enactment of the present, « Gregorian » calendar.

Contrary to fanciful allegations in a recent best-selling novel, this is not a vestige of pagan temple. No such temple ever existed in this place. It was never called a « Rose-Line ». It does not coincide with the meridian traced through the middle of the Paris Observatory which serves as a reference for maps where longitudes are measured in degrees East or West of Paris. No mystical notion can be derived from this instrument of astronomy except to acknowledge that God the Creator is the master of time.

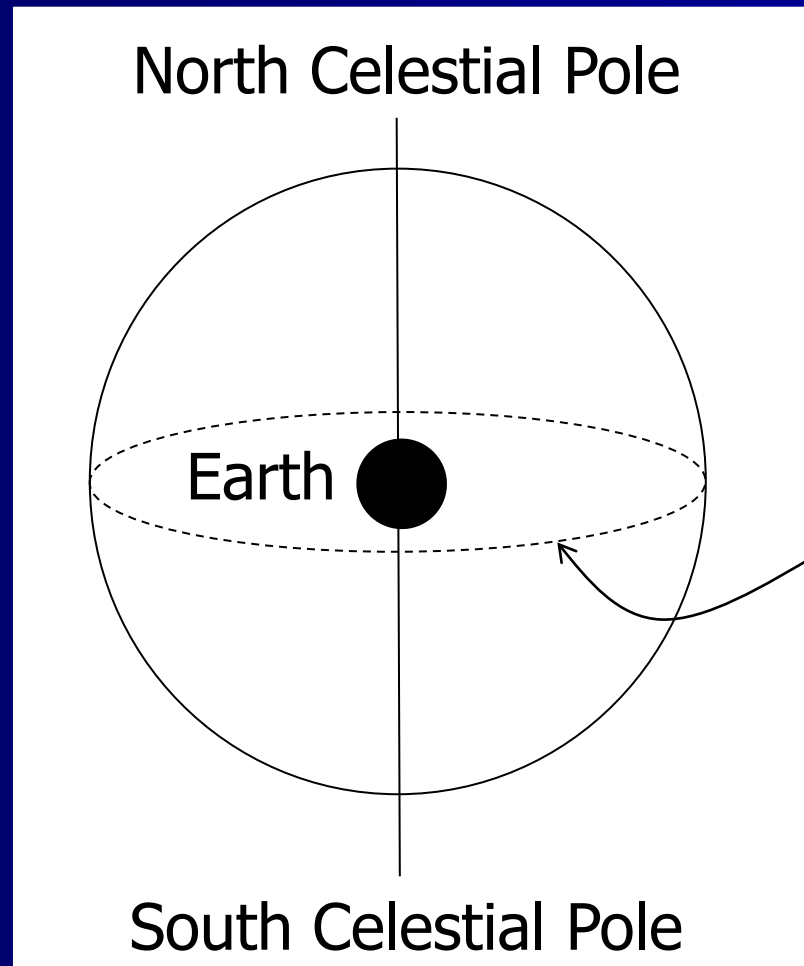
Please also note that the letters « P » and « S » in the small round windows at both ends of the transept refer to Peter and Sulpice, the patron saints of the church, not an imaginary « Priory of Sion ».

La « ligne
réglette de la
fait partie
« gnomon ast
par les resp
plain accord
vue de mesu
terre autour
genre ont «
grandes égli
le pape Grég
les études p
calendrier «

Contraire
contenues d
méridienne
d'un temple
ne l'a jamais
pas avec le
référence au
degrés ou
La seule m
instrument
Créateur et

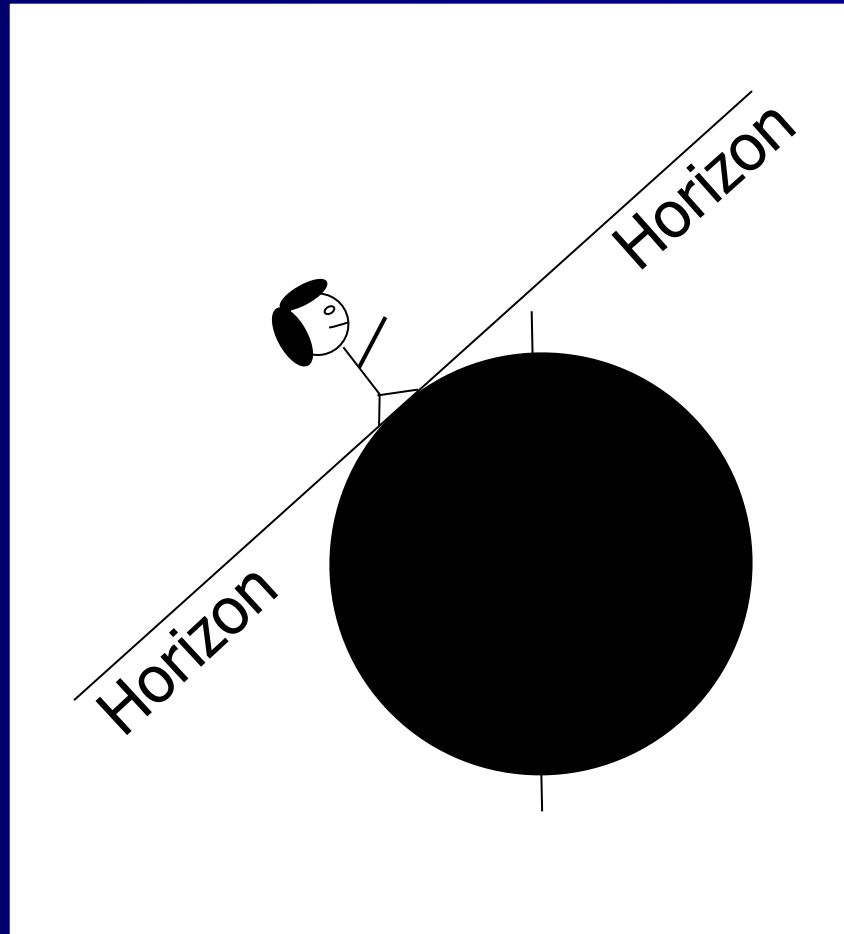
Veuille
sur les fen
transept, s
qui sont l
« Prieuré d

To Understand Meridian Lines, Start with the Celestial Sphere

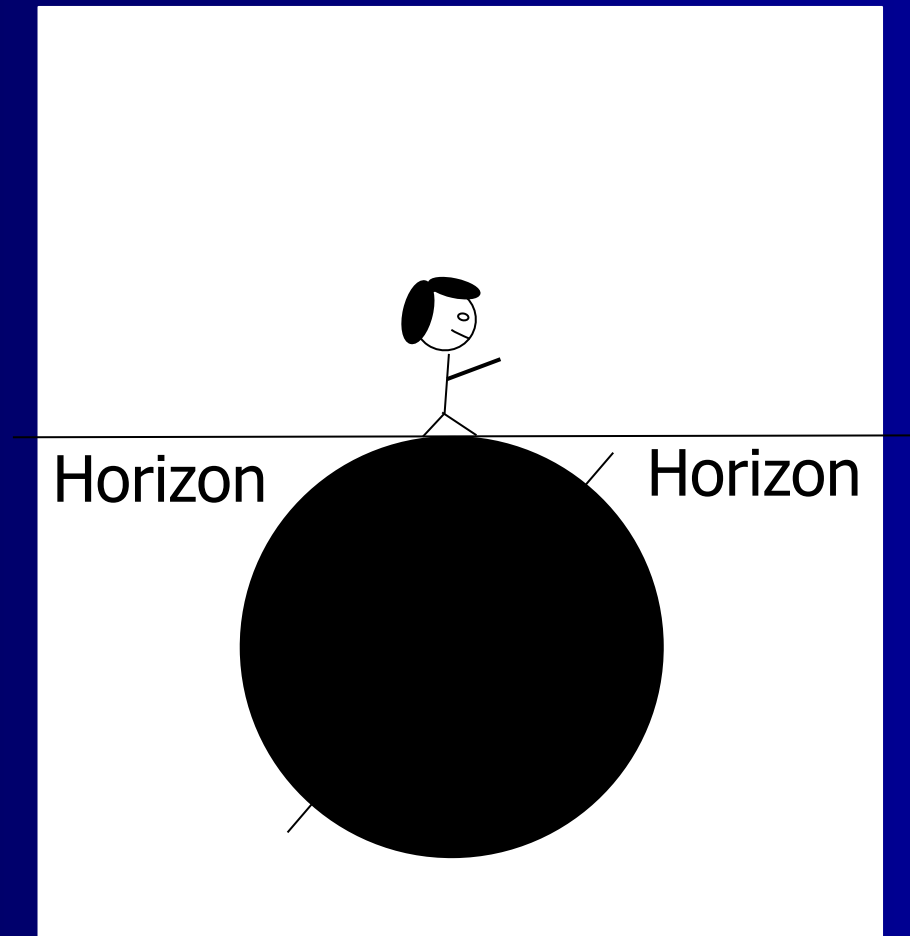


Celestial
Equator

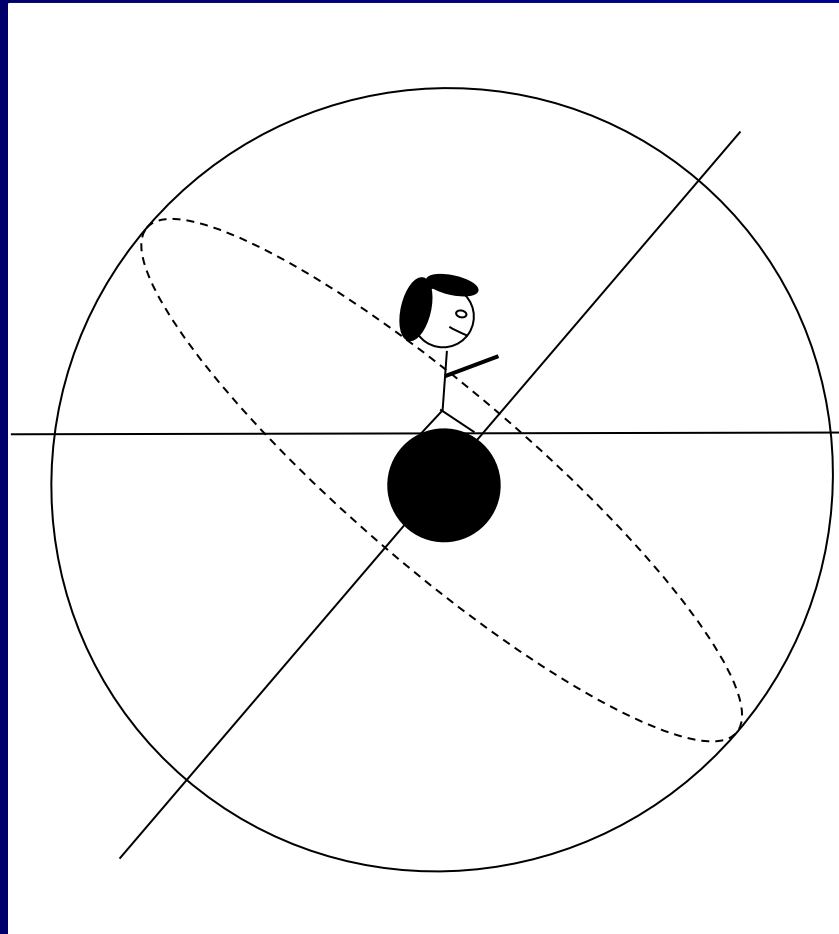
To Understand the Celestial Sphere, Start with a Giant Girl on Earth



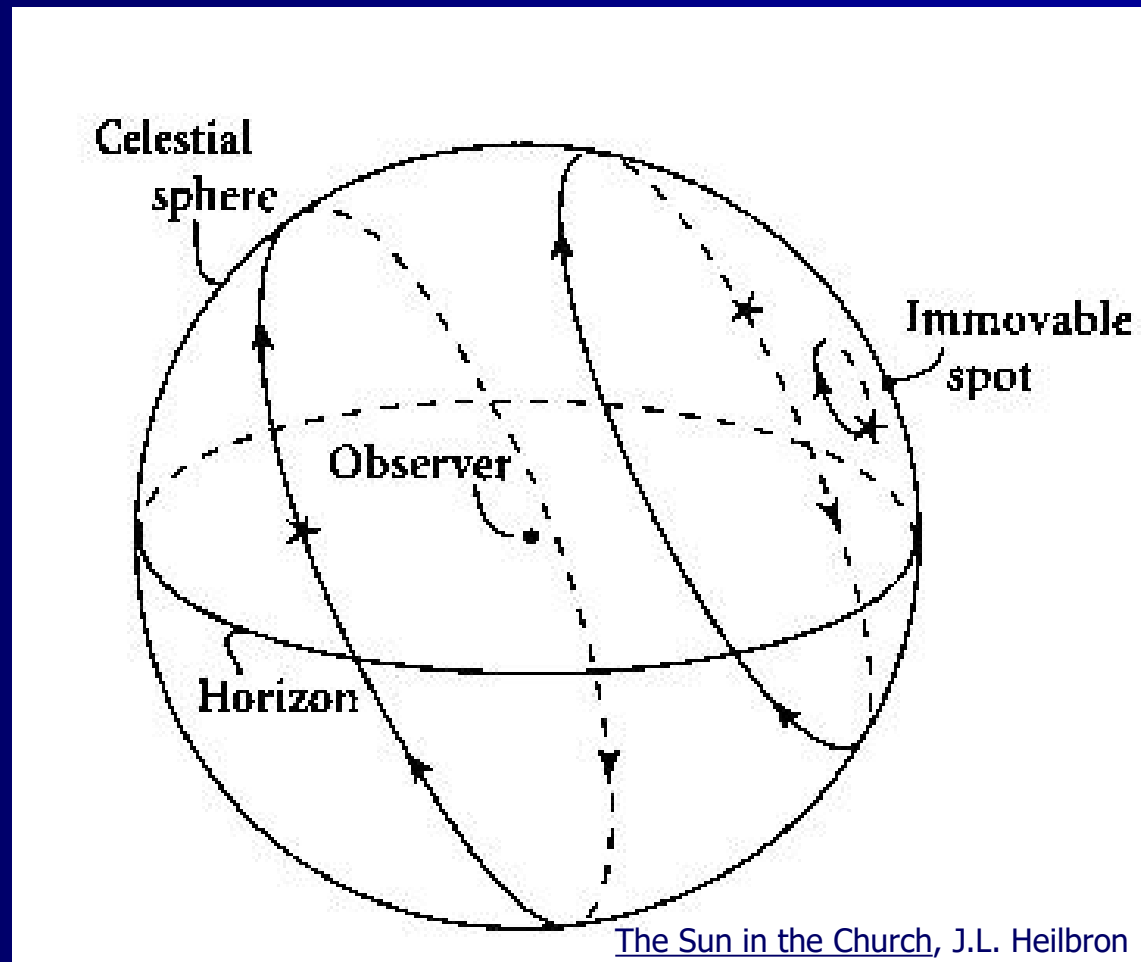
The Giant Girl Believes She's on Top of the World



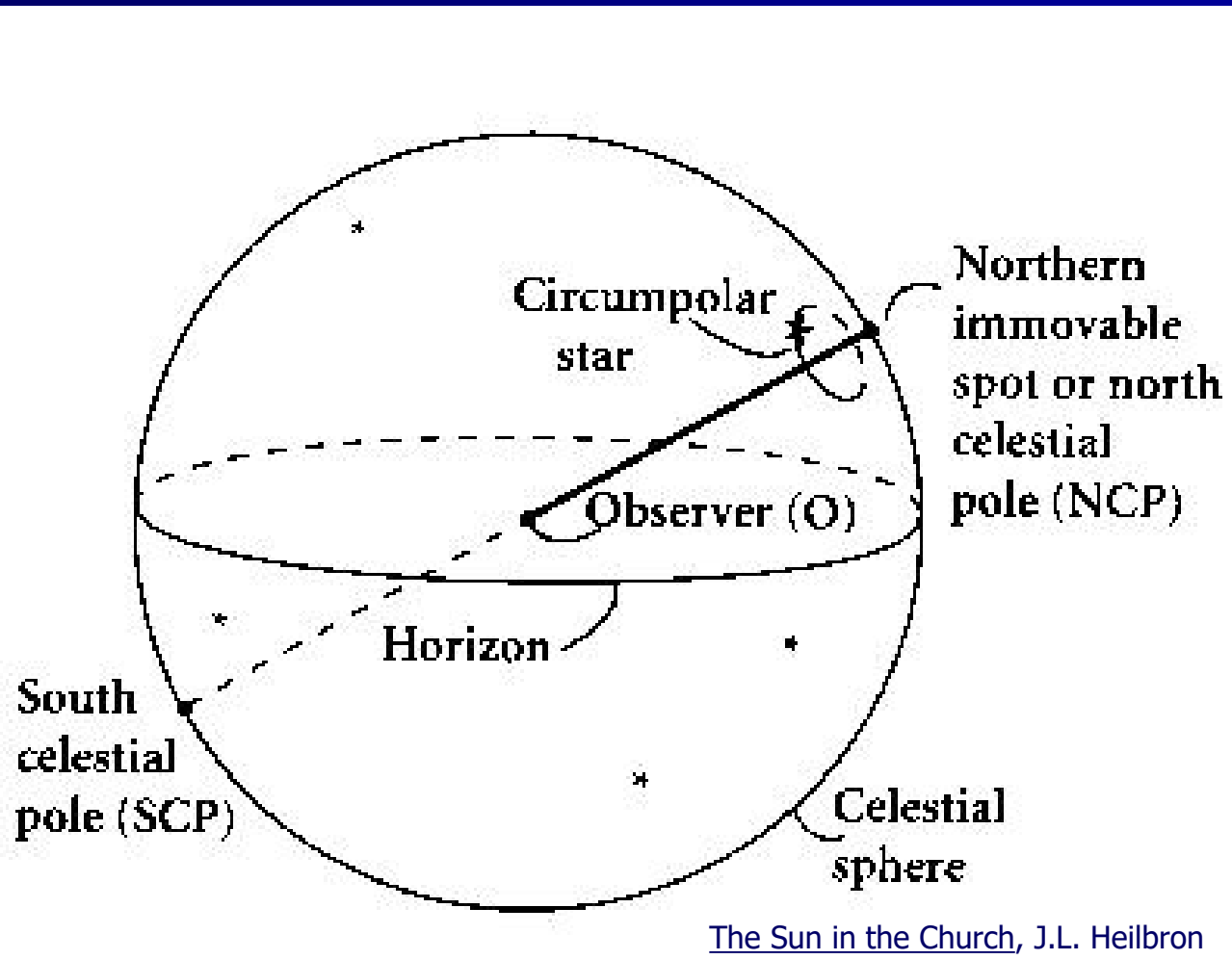
The Giant Girl's Celestial Sphere



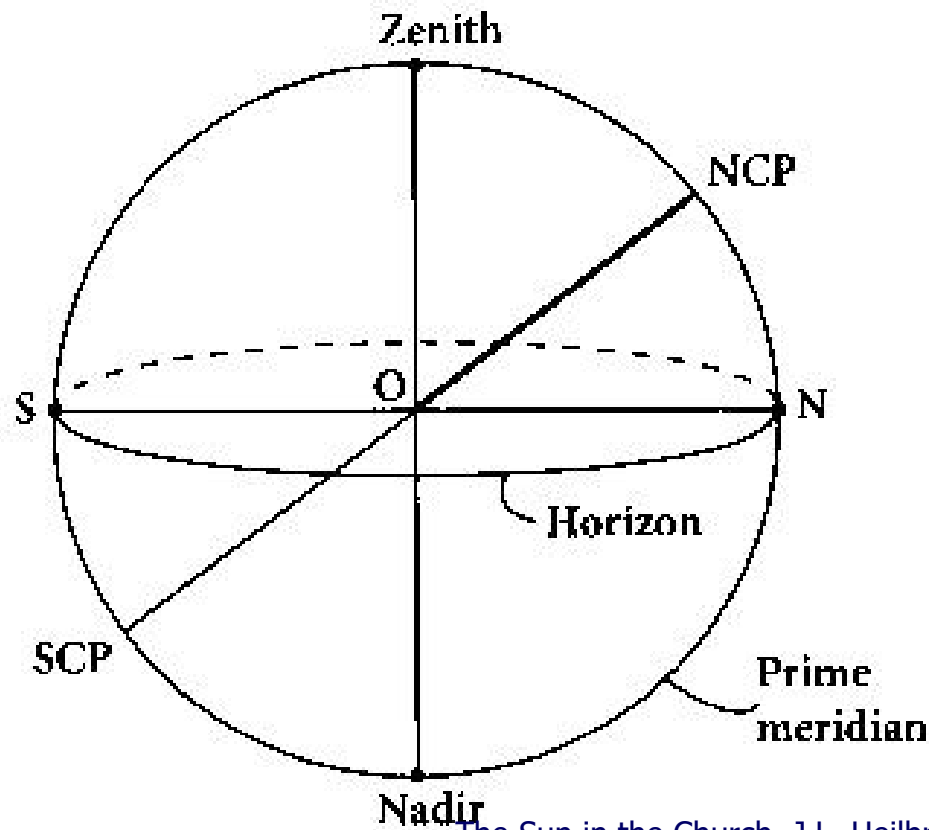
The Celestial Sphere as Usually Drawn



Circumpolar Stars

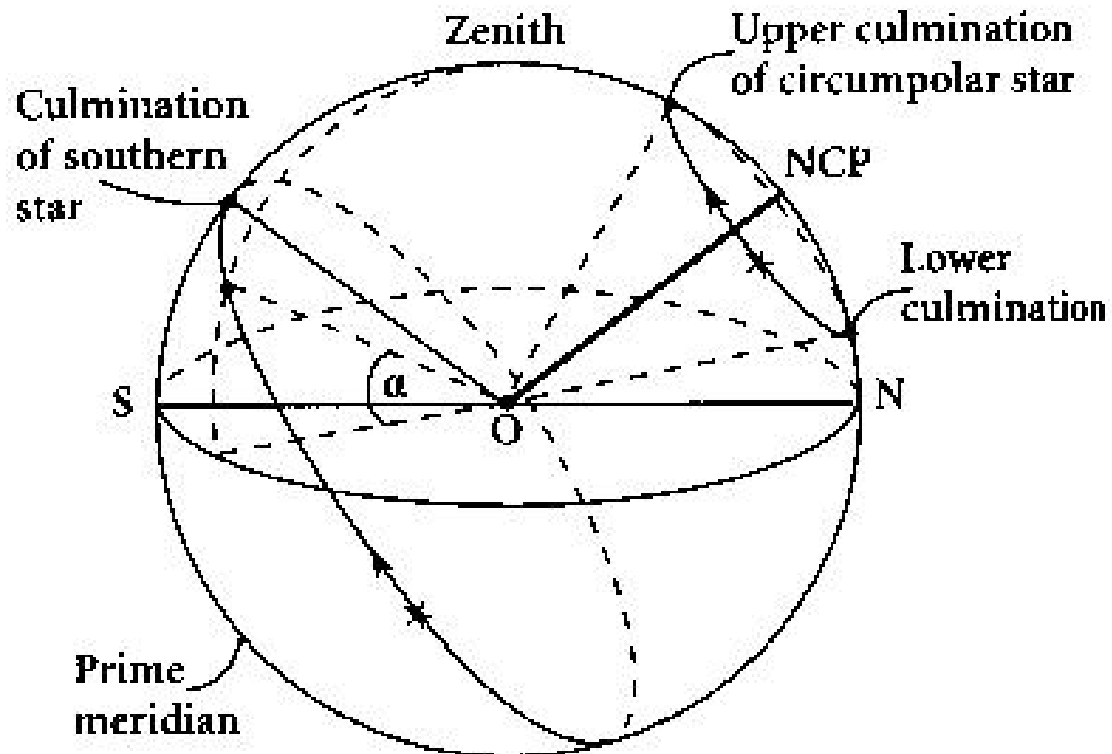


Celestial Sphere Terminology



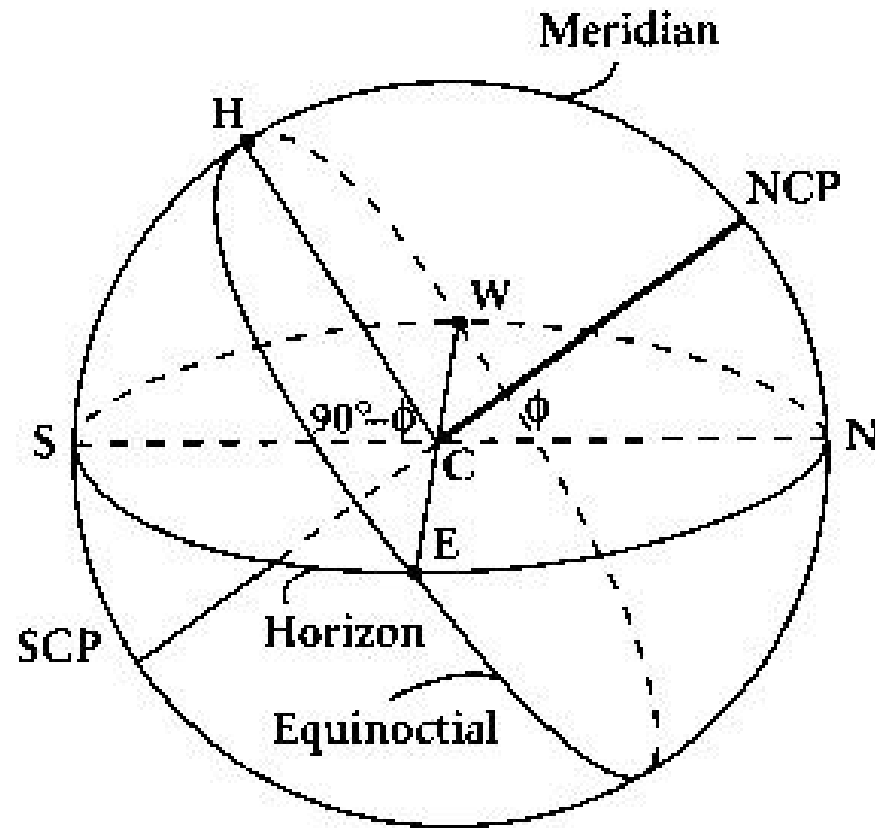
[The Sun in the Church, J.L. Heilbron](#)

Culmination



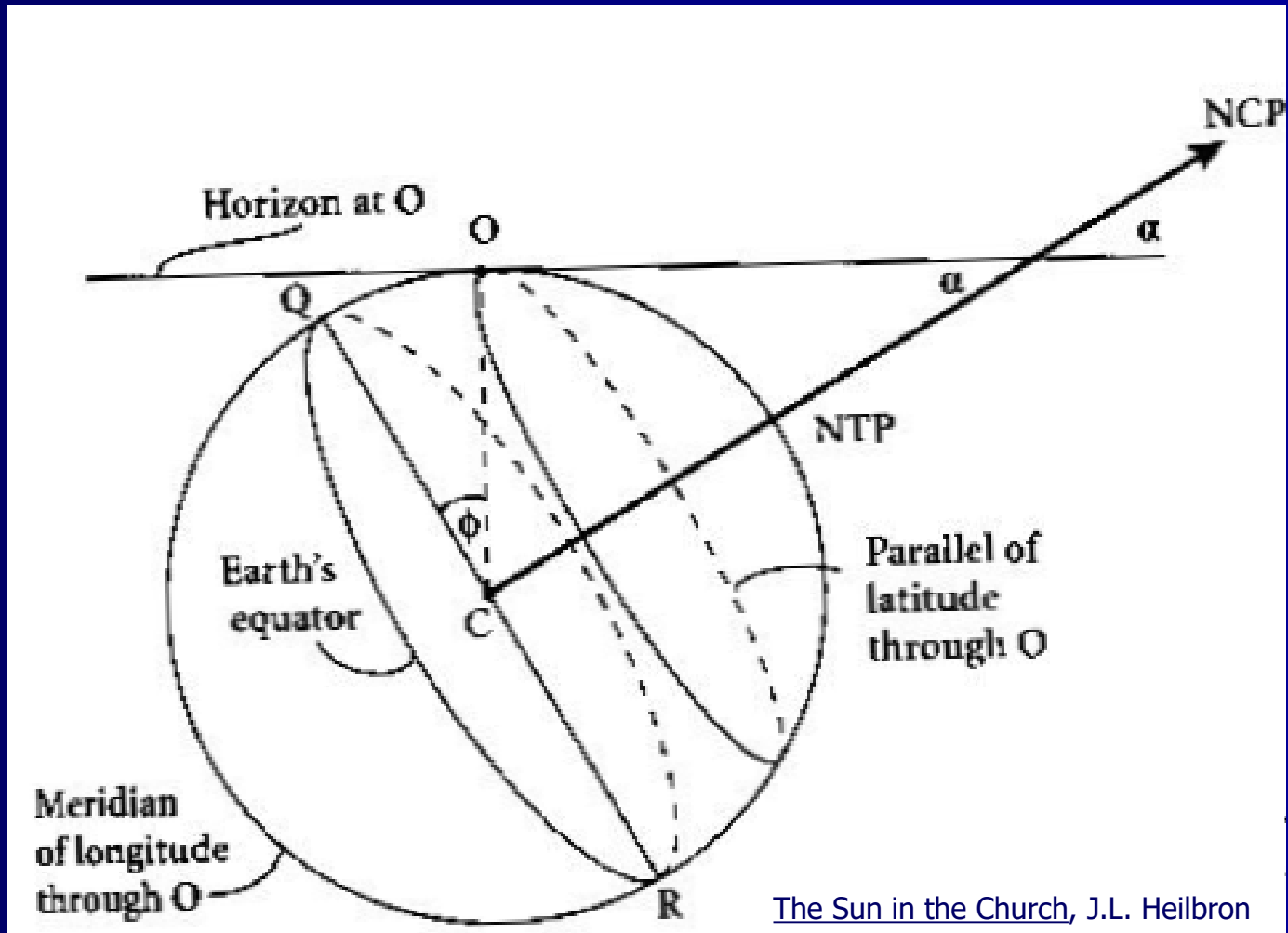
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Halfway Between the Poles: the Equinoctial

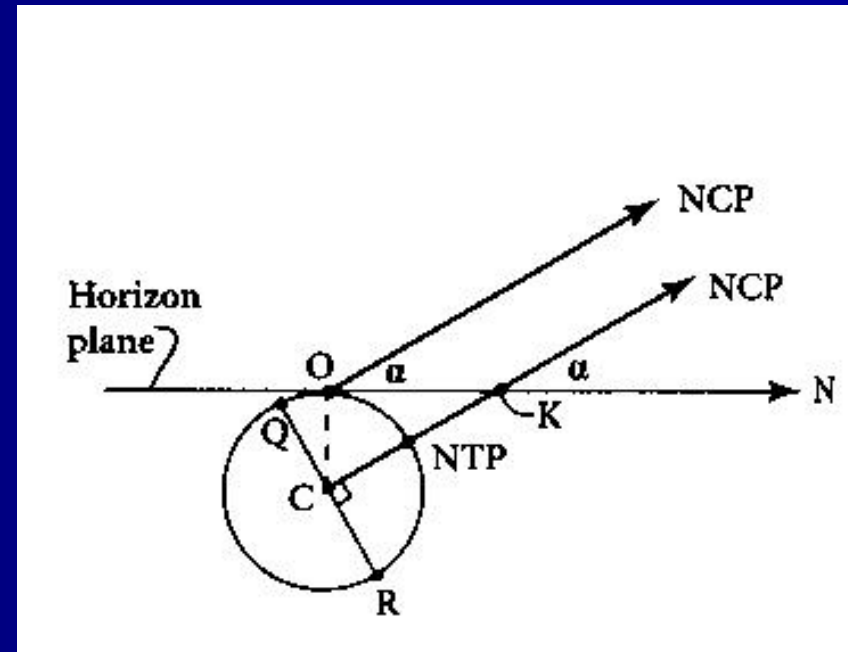
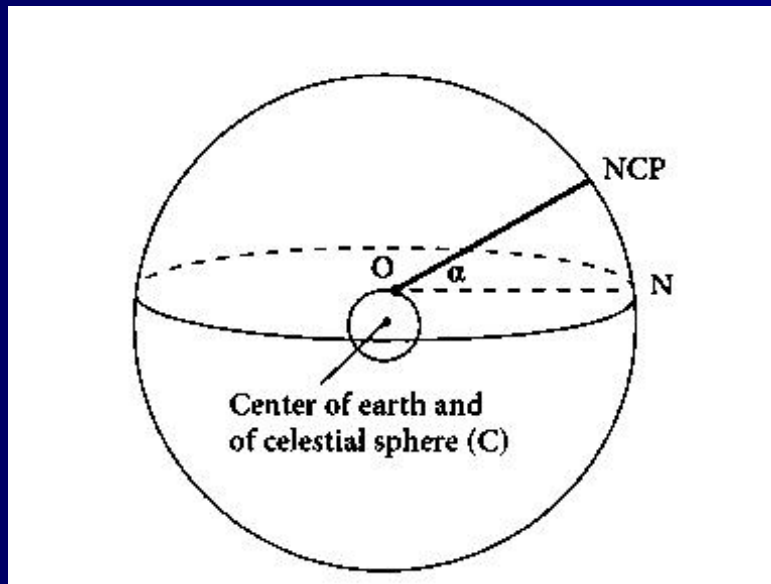


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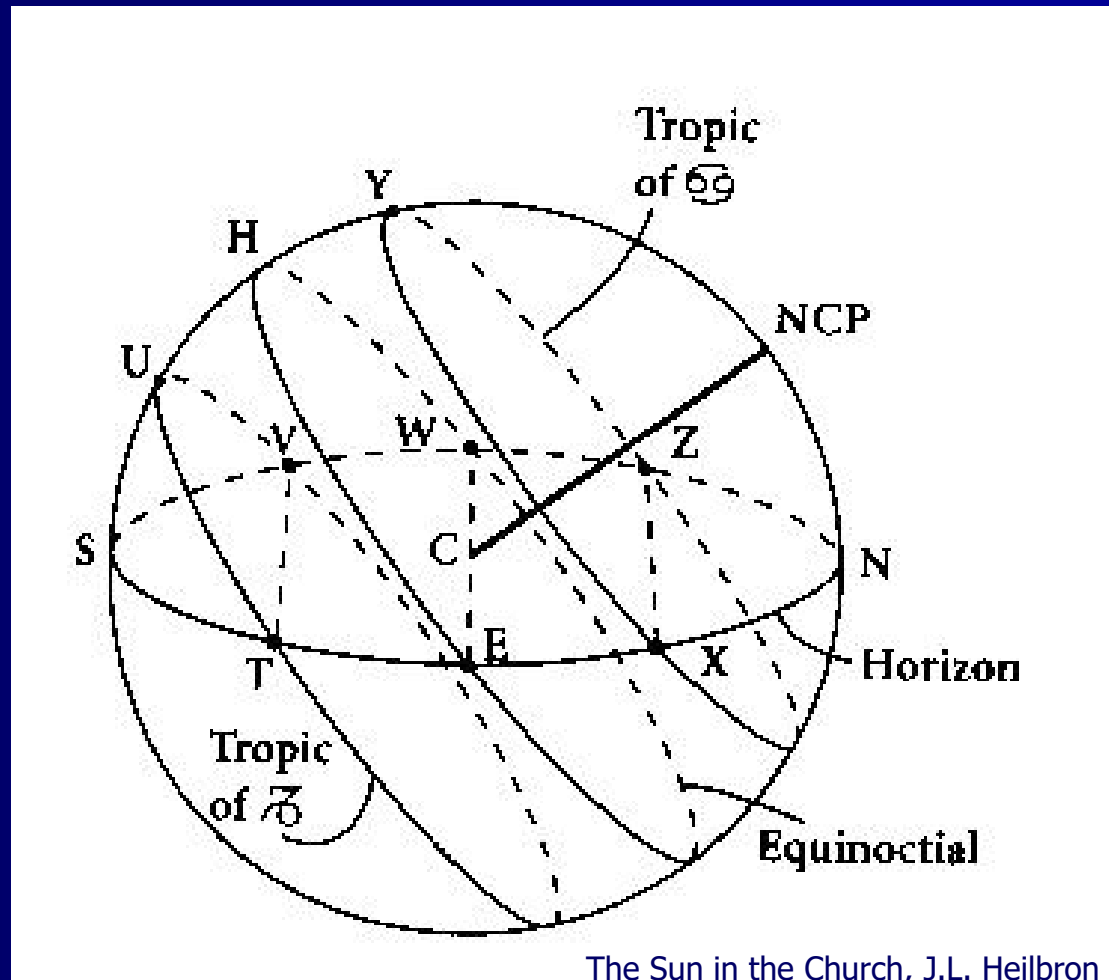
Finding Latitude is Easy



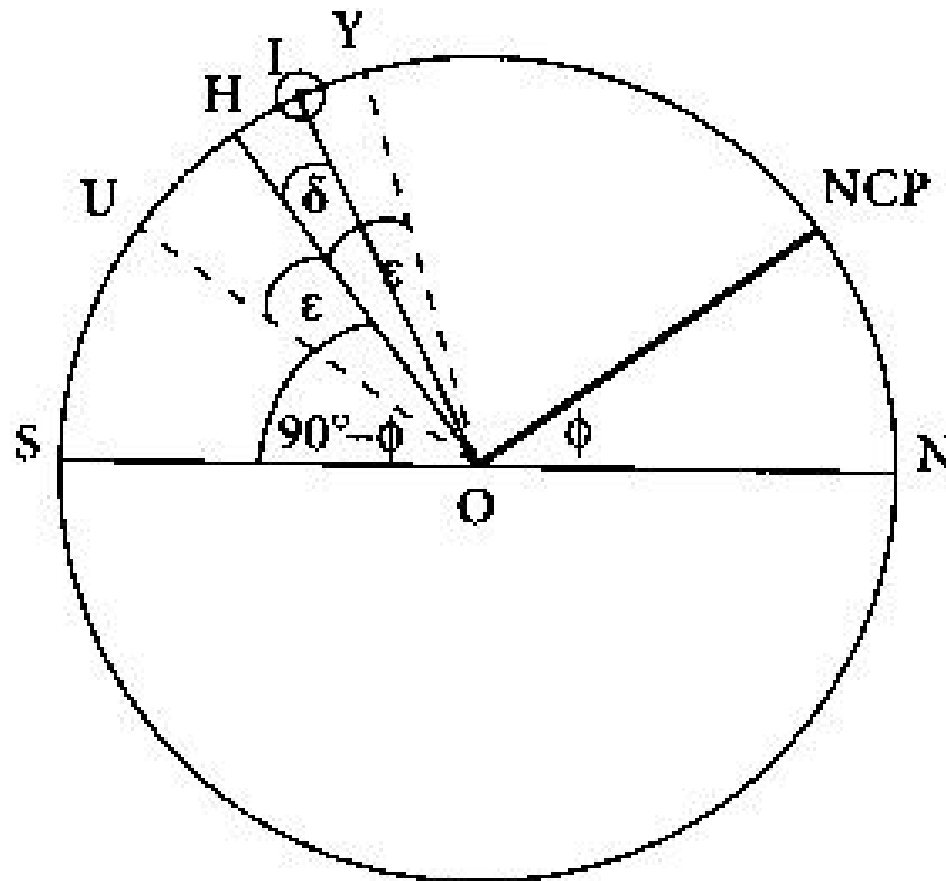
For Stars, Parallax is Negligible over Earth's Surface



The Sun's Position on the Celestial Sphere



Highest in the South, Highest in the Summer



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Correction: Refraction

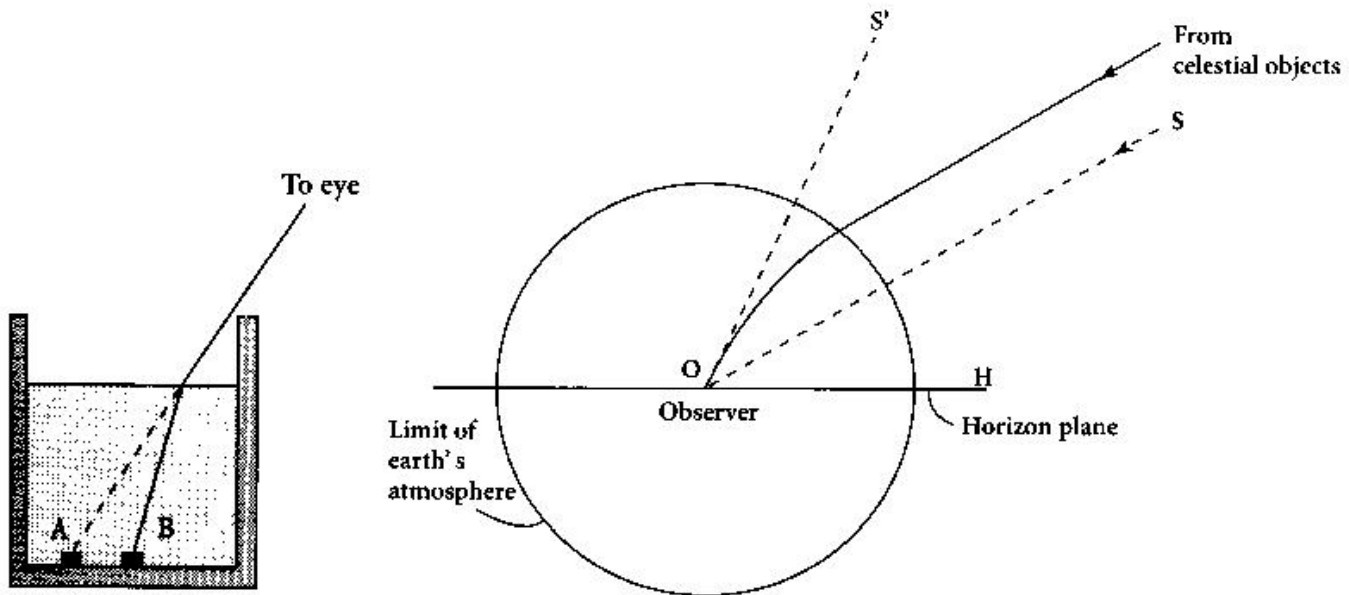


FIG. 3.6. A familiar example of refraction in water; the coin appears to the left of its true position.

FIG. 3.7. The effect, much exaggerated, of refraction on astronomical observation; the star appears at S' rather than at S to the observer O.

Correction: Solar Parallax

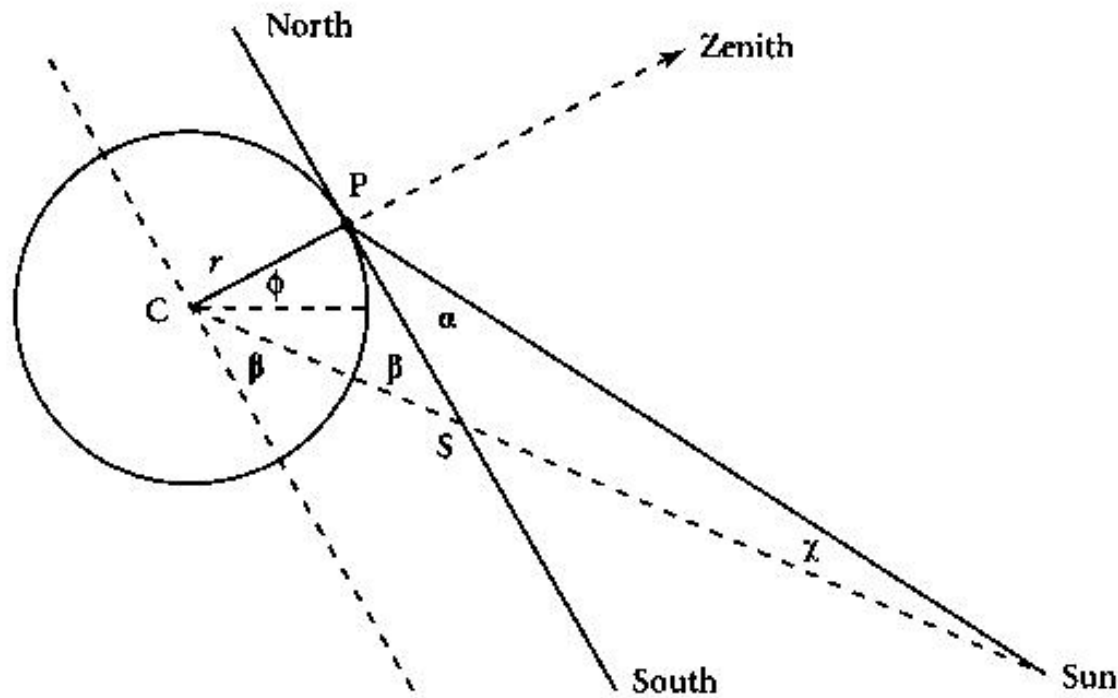


FIG. 3.8. Definition of solar parallax χ .

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Bisecting the Eccentricity

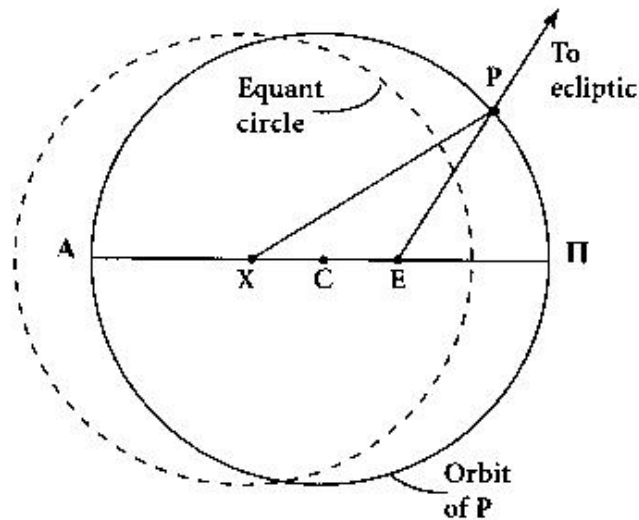


FIG. 3.13. Eccentric and equant X; the eccentricity is bisected, $XC = CE = ae/2$.

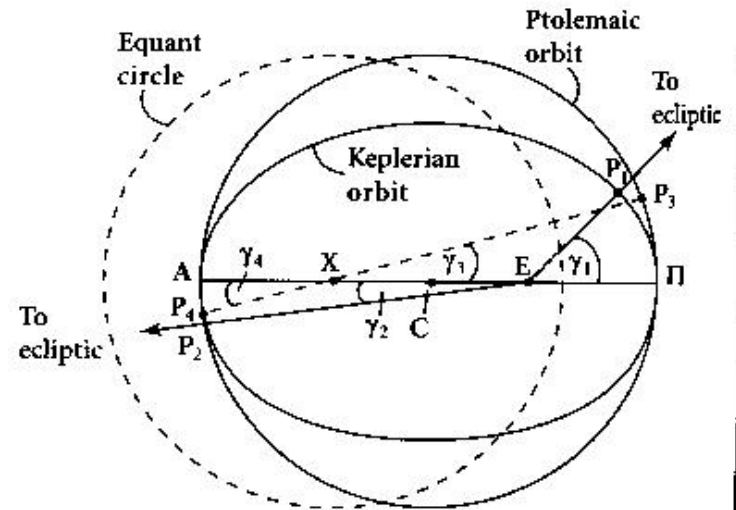


FIG. 3.14. A Ptolemaic circular orbit with eccentric and equant compared with a Keplerian ellipse.

A Factor of Two in Change of Image Size

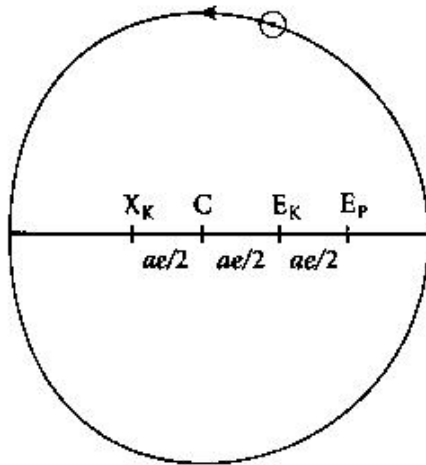


FIG. 3.16. Comparison of apsidal distances in Ptolemy's and Kepler's representations of the sun's orbit.

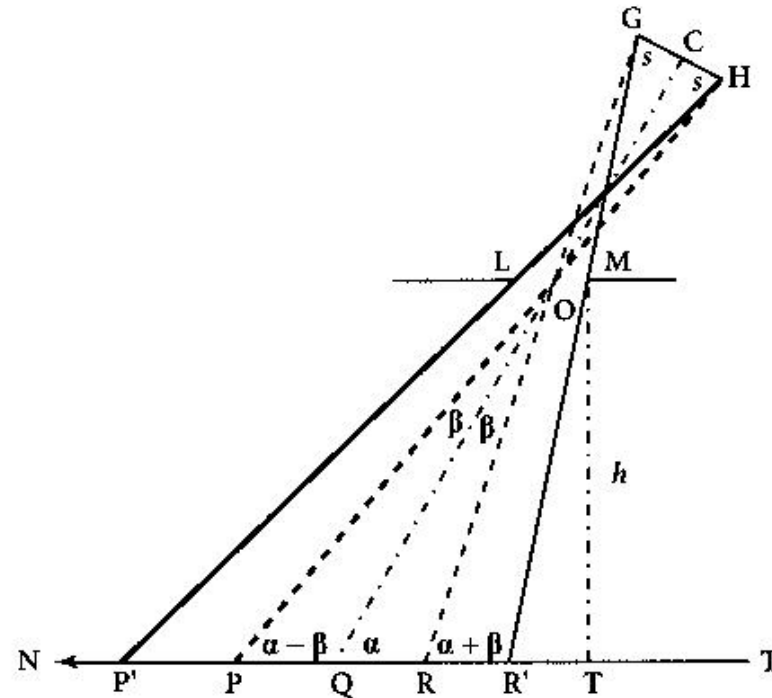
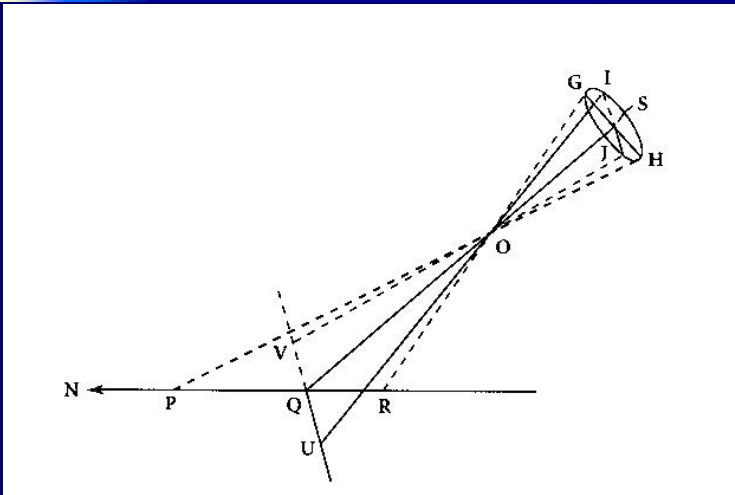
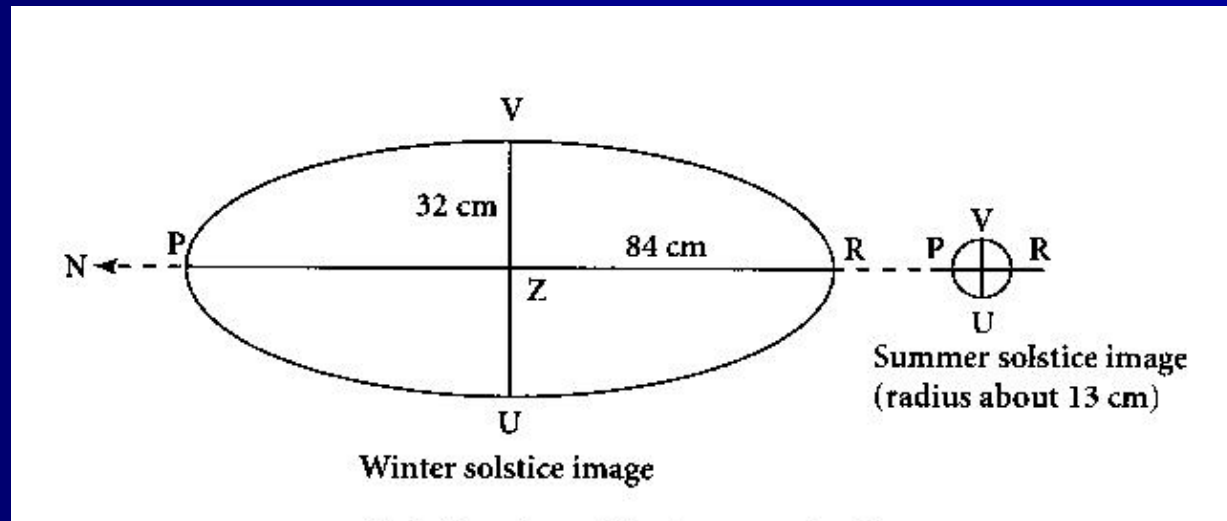


FIG. 3.17. Longitudinal diameter ($P'R'$) of the sun's image in San Petronio.

The Size of the Spot



The Sun in the Church, J.L. Heilbron



The Result

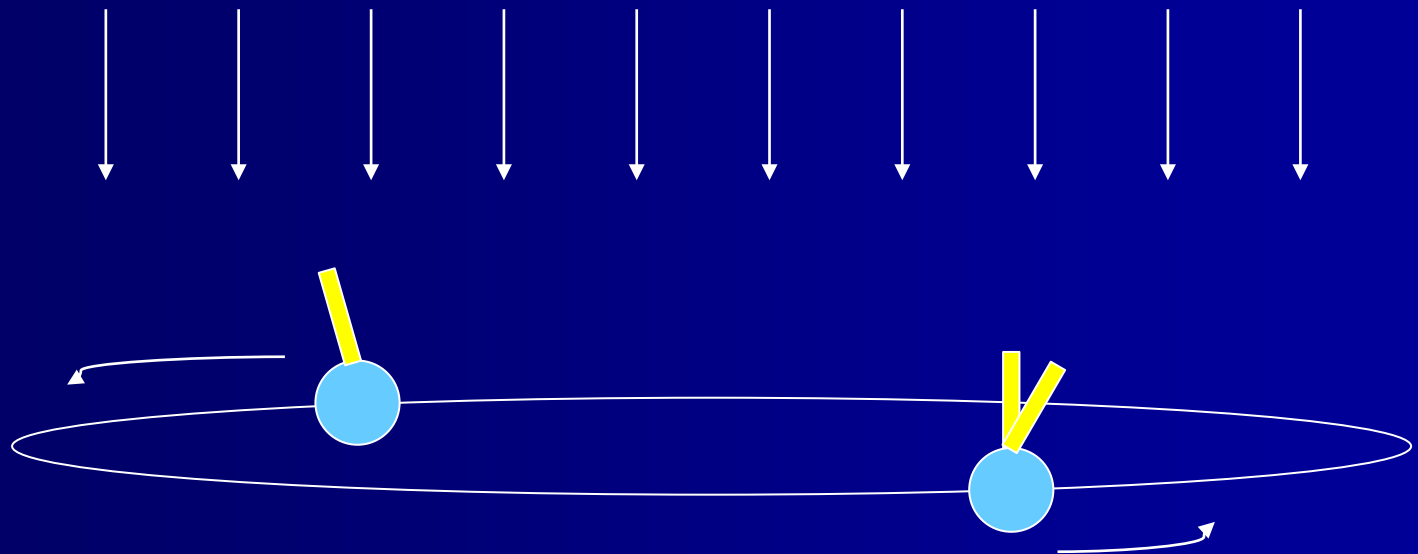
- Ptolemaic Model predicts image size change of 2' between solstices
- Keplerian Model predicts image size change of 1' between solstices
- The meridian line measurement:
Image size changes by 1'

Overwhelming Evidence in Favor of Kepler and Moving Earth

- Meridian lines provide accurate timing to about 1 second per year, and elliptical (rather than circular) models fit the data
- Telescopic observations reveal the aberration of starlight

Aberration of Starlight

Starlight



Earth

So...

The evidence gathered by priest-astronomers using Church-funded meridian lines and other instruments eventually rendered the concept of purely circular motion, perfect heavenly orbs, and the Earth-centered Universe untenable.

Progress

1822: Church removes ban on Galileo's books

1992: Pope John Paul II acknowledges that Galileo's imprisonment had been a mistake caused by "tragic mutual mis-comprehension."

And While They Were At It ...

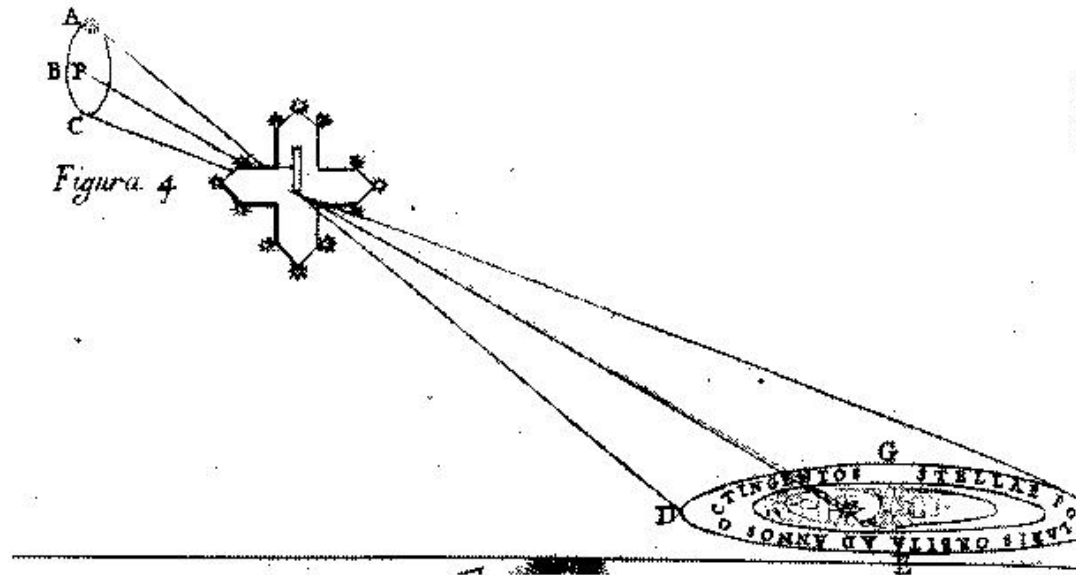
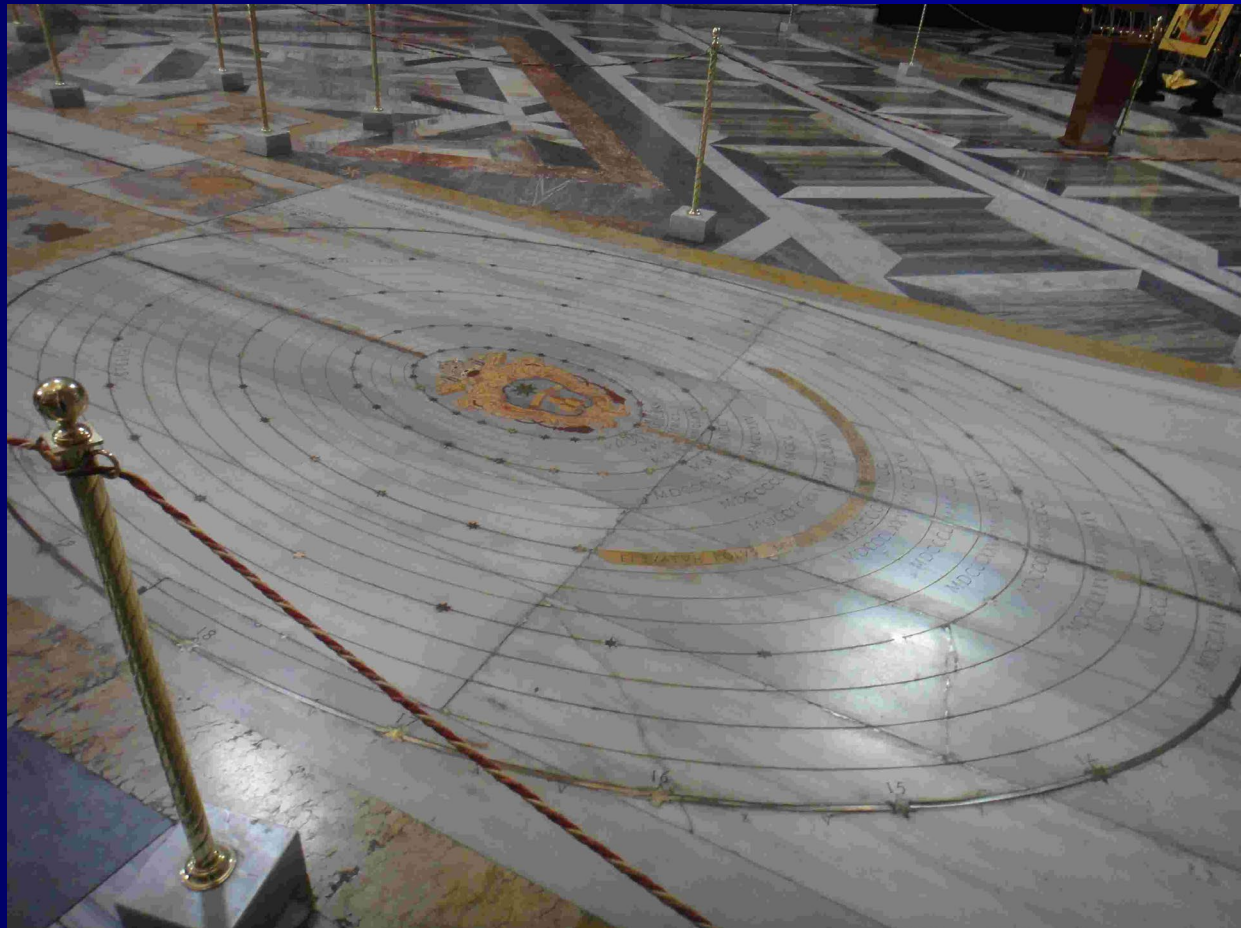
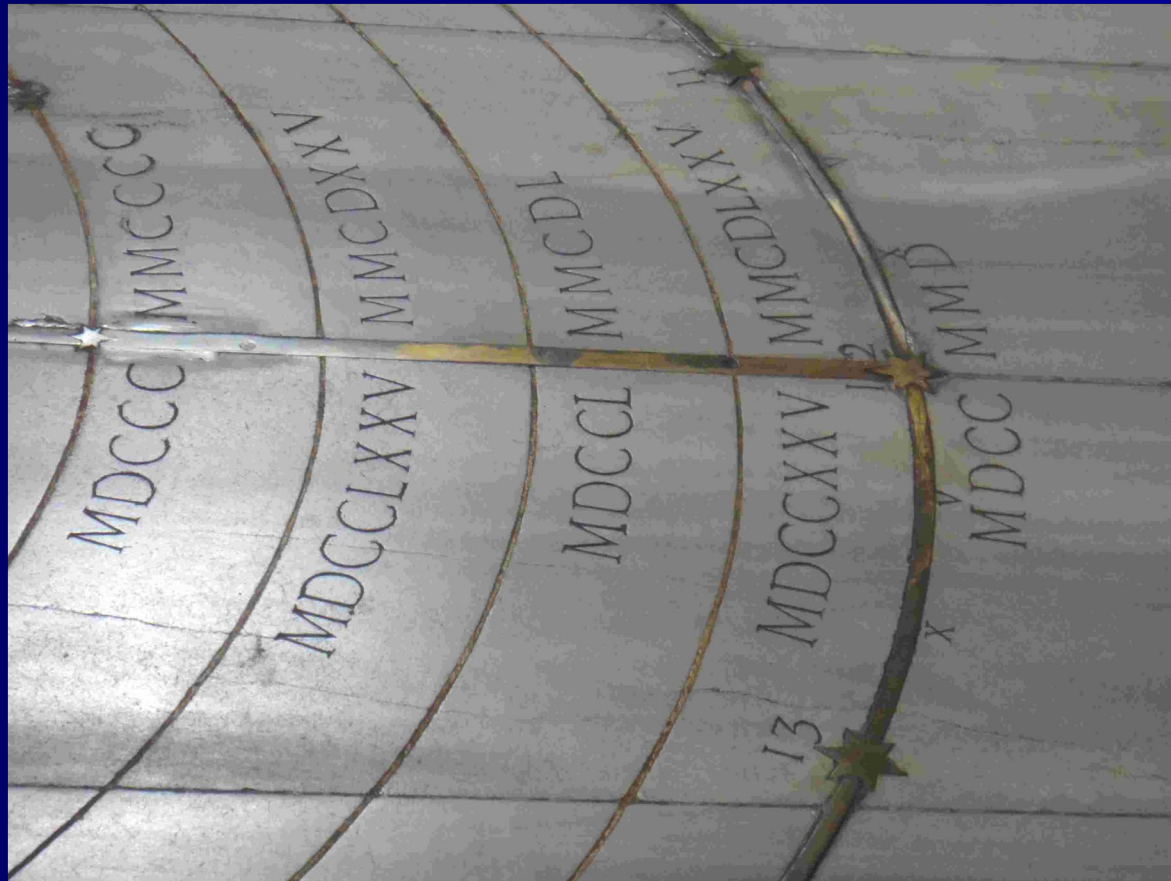


FIG. 5.7. The northern gnomon at S. M. degli Angeli, Rome. ABC indicates Polaris' diurnal orbit, GDE its image on the pavement. The Latin says "the polestar's orbits for 800 years." From Bianchini, *De nummo* (1703).

Polaris and the Celestial Pole



The Long View



Read More About It

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Harvard University Press (1999)

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